



Arley Primary School Calculation Policy

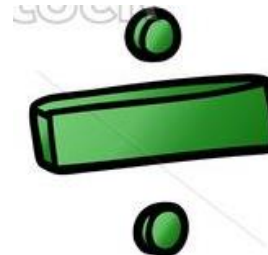
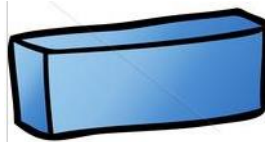


This policy supports the White Rose maths scheme used throughout the school. Progression within each area of calculation is in line with the programme of study in the 2014 National Curriculum. This calculation policy should be used to support children to develop a deep understanding of number and calculation. This policy has been designed to teach children through the use of concrete, pictorial and abstract representations.

- Concrete representation - a pupil is first introduced to an idea or skill by acting it out with real objects. This is a 'hands on' component using real objects and is a foundation for conceptual understanding.
- Pictorial representation - a pupil has sufficiently understood the 'hands on' experiences performed and can now relate them to representations, such as a diagram or picture of the problem.
- Abstract representation - a pupil is now capable of representing problems by using mathematical notation, for example $12 \times 2 = 24$.

It is important that conceptual understanding, supported by the use of representation, is secure for all procedures.

Reinforcement is achieved by going back and forth between these representations.




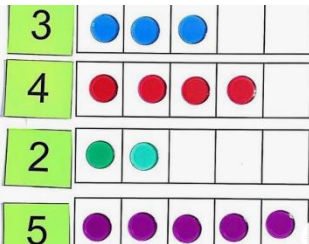

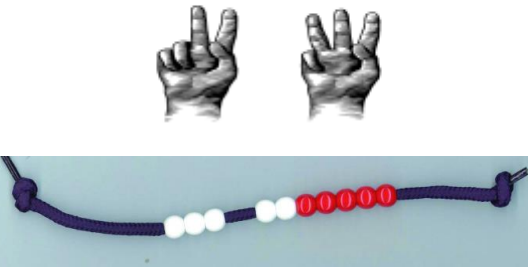
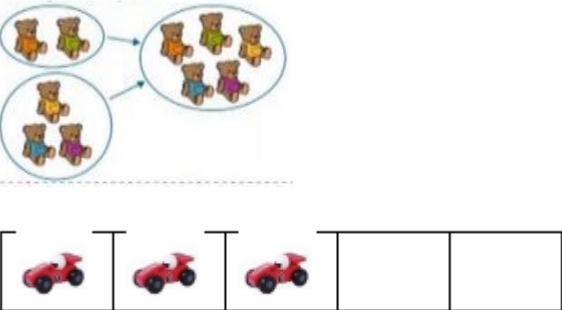
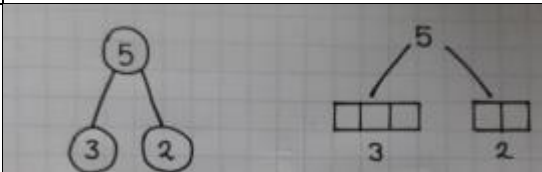
Updated March 2022

J.Mackley

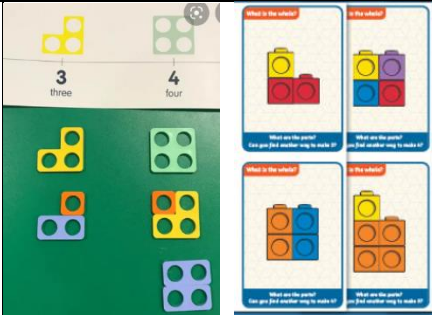


Addition Guidance



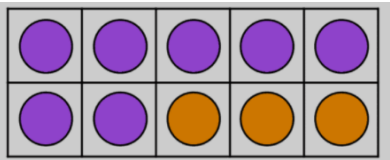
EYFS – Addition			
Vocabulary: fives frame, tens frame, whole, part, add, plus, greater than, less than, the same as, most, least, bigger, smaller, equal			
Helpful Videos/Resources: https://www.ncetm.org.uk/classroom-resources/ey-numberblocks-support-materials/			
Method:	Concrete:	Pictorial:	Abstract:
Subitise (recognise quantities without counting) up to 5	 <p>Use toys and general classroom resources for children to physically manipulate, group/regroup.</p>	<p>Use fives frames to sort objects/counters</p> 	<p>Relationships between pictures and objects as numerals</p> 
Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 and some number bonds to 10	<p>Show me 5 fingers using both hands.</p> 	 <p>How many have we got? What is our whole? How many spaces are there? How many could we have?</p>	 <p>Using both of these representations for number bonds will ensure children are provided with variation in their representations and also begin to build foundations for independently drawing these in Year 1. A large emphasis is placed on the part and whole vocabulary.</p>

Have a deep understanding of number to 10, including the composition of each number



Represent numbers in different ways using numicon/other resources eg. Multilink

Use of tens frames to sort objects/counters



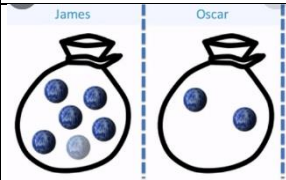
Relationships between pictures and objects as numerals and words



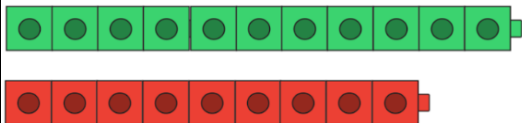
Compare quantities up to 10 in different contexts, recognising when one quantity is greater than, less than or the same as the other quantity



Use of balance scales to compare number of objects (items such as numicon are weighted correctly for this).



_____ has the most marbles.

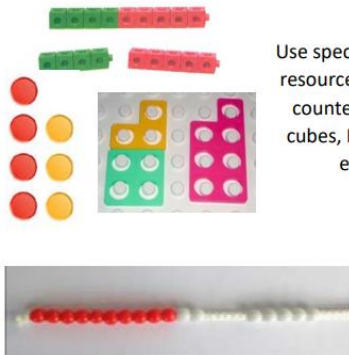
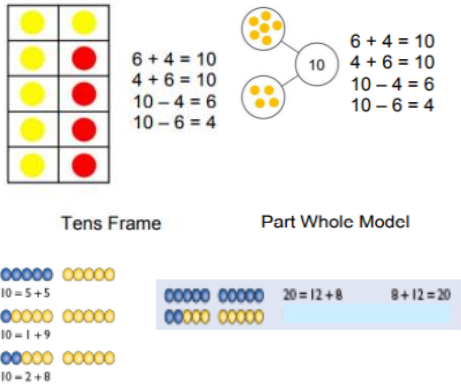
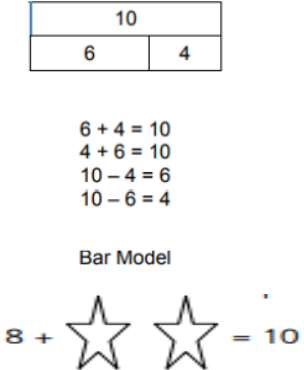
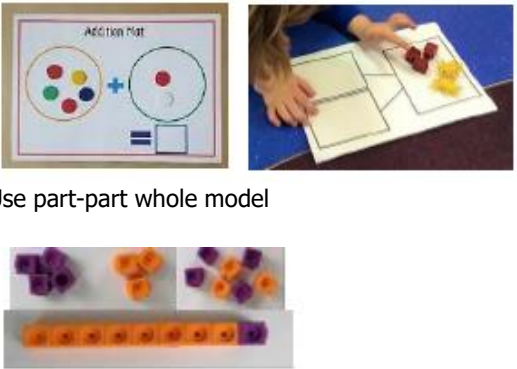
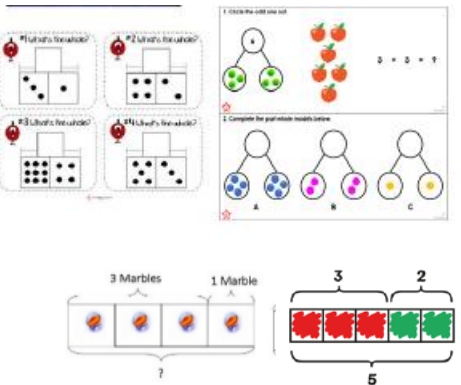
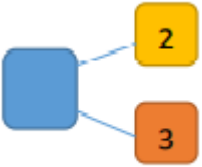


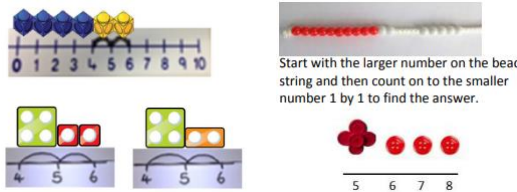
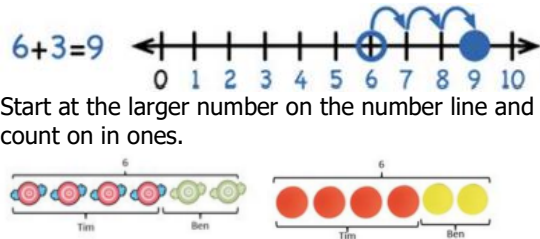
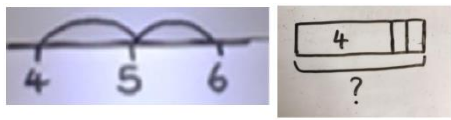

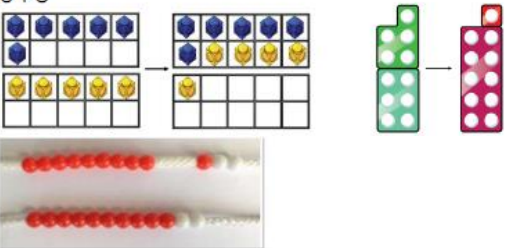
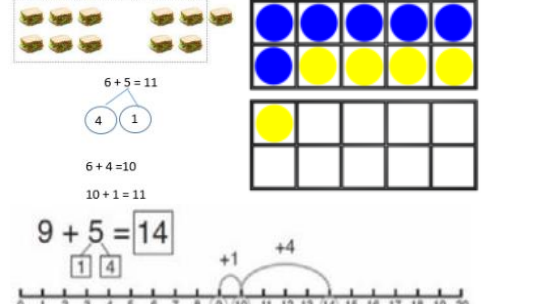
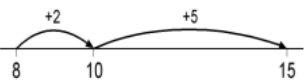
Which tower is bigger/smaller?



MENTAL STRATEGIES:

- Verbally count beyond 20

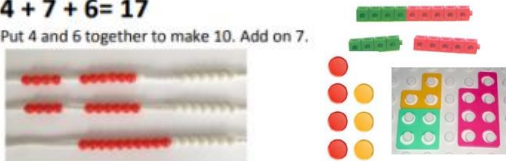
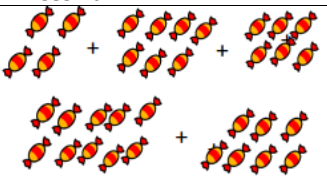
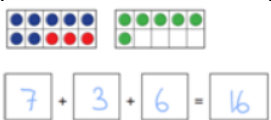
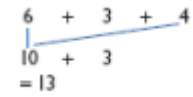

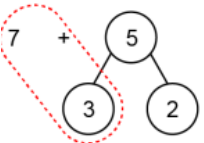
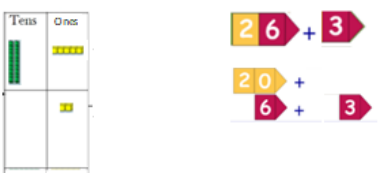
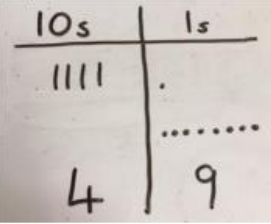
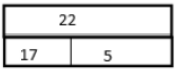
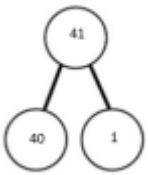
Year 1 – Addition			
Vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, balancing, part, part, whole			
Helpful Videos/Resources: https://www.ncetm.org.uk/classroom-resources/cp-year-1-curriculum-map/ , https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/ , https://www.ncetm.org.uk/media/qjpctp24/mastery_assessment_y1.pdf , https://whiterosemaths.com/resources?year=year-1			
Method:	Concrete:	Pictorial:	Abstract:
Represent and use number bonds and related subtraction facts within 20	 <p>Use specific maths resources such as counters, snap cubes, Numicon etc.</p>	 <p>Tens Frame Part Whole Model</p>	 <p>Bar Model</p>
Combining two parts to make a whole: part whole model.	 <p>Use part-part whole model</p> <p>Use cubes to add two numbers together as a group or in a bar. (Some children may still need to use real objects)</p>	 <p>The Bar Model will be continued from EYFS as a method to support problem solving involving addition, continuing with the concrete representations and moving onto using pictorial representations of objects.</p>	A focus on symbols and numbers to form a calculation and fact families. $2 + 3 = 5$ $3 + 2 = 5$ $5 - 3 = 2$ $5 - 2 = 3$ 

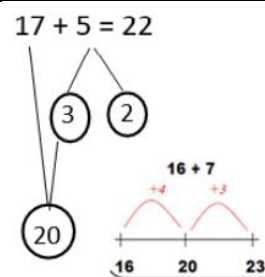
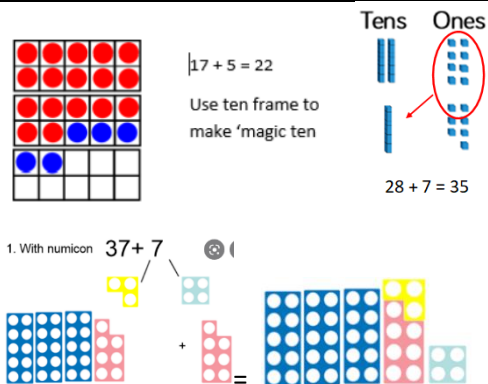
<p>Starting at the bigger number and counting on.</p>	 <p>Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.</p>	<p>$6 + 3 = 9$</p>  <p>Start at the larger number on the number line and count on in ones.</p>	 <p>$3 + \square = 5$</p> 
<p>Regrouping to make 10</p> <p>*Regrouping builds on pupils' understanding that 10 ones is equivalent to 1 ten</p>	<p>$6 + 5$</p>  <p>Start with the bigger number and use the smaller number to make 10.</p>	 <p>$6 + 5 = 11$</p> <p>$6 + 4 = 10$</p> <p>$10 + 1 = 11$</p> <p>$9 + 5 = 14$</p>	<p>$6 + 5 = 11$</p> <p>$6 + 4 = 10$</p> <p>$10 + 1 = 11$</p> <p>$8 + 7 = 15$</p> 
<p>MENTAL STRATEGIES:</p> <ul style="list-style-type: none"> - Memorise and reason with number bonds to 10 and 20 in several forms (for example, $9 + 7 = 16$; $16 - 7 = 9$; $7 = 16 - 9$) - Realise the effect of adding or subtracting zero - Combine and increase numbers, counting forwards and backwards 			

Year 2 – Addition

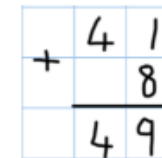
Vocabulary: add, addition, more, plus, make, sum, total, altogether, score, double, near double, one more, two more ... ten more...one hundred more, how many more to make...?, how many more is... than...?, how much more is...?, tens boundary

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-2-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/> , https://www.ncetm.org.uk/media/dnbt14/mastery_assessment_yr2.pdf , <https://whiterosemaths.com/resources?year=year-2>

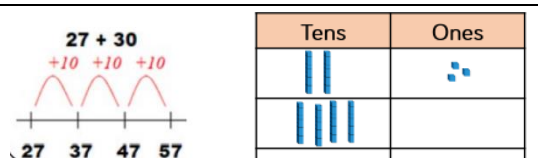
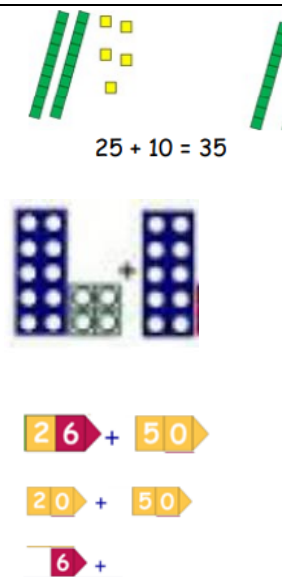
Method:	Concrete:	Pictorial:	Abstract:
Adding 3 1-digit numbers	<p>4 + 7 + 6 = 17</p> <p>Put 4 and 6 together to make 10. Add on 7.</p>  <p>Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit. Could use counters, cubes, numicon etc.</p>	 <p>Add together three groups of objects. Draw a picture to recombine the groups to make 10.</p> 	  <p>Children should relate adding 3 numbers to adding 2 numbers e. $7 + 3 + 2 = 7 + 5$</p> 
Adding a 2-digit number and ones *Regrouping and exchange build on pupils' understanding that 10 ones is equivalent to 1 ten. Base 10/tens frames/Numicon can be used to model the calculations, and to draw attention to the regrouping/exchange.	<p>Continue to develop understanding of partitioning and place value using base 10 and place value grids:</p> <p>$25 + 2$</p>  <p>Use 10's frames, numicon and base 10 to build on knowledge of regrouping:</p>		<p>Explore related facts</p> <p>$17 + 5 = 22$ $5 + 17 = 22$ $22 - 17 = 5$ $22 - 5 = 17$</p>  <p>41 + 8</p>  <p>$1 + 8 = 9$ $40 + 9 = 49$</p> <p>*Pupils do not need to learn formal written methods for addition and subtraction in year 2,</p>



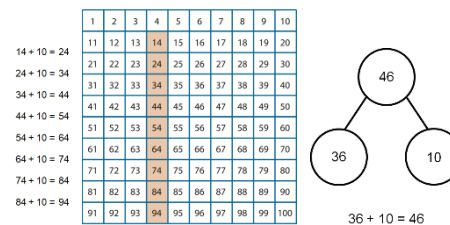
but column addition and column subtraction could be used as an alternative way to record two-digit calculations at this stage.



Adding a 2-digit number and multiples of 10

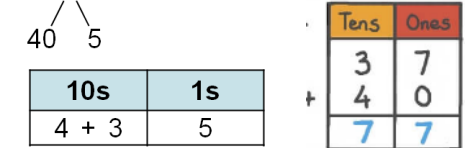


Base 10 may be used above the number line initially.



*Ensure understanding that the ones digit does not change with all representations

$$45 + 30 = 75$$



$$27 + 10 = 37$$

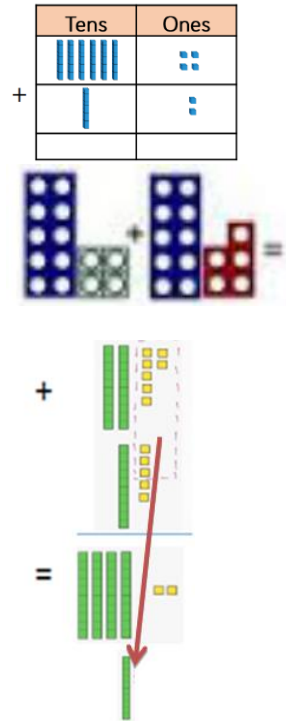
$$27 + 20 = 47$$

$$27 + \square = 57$$

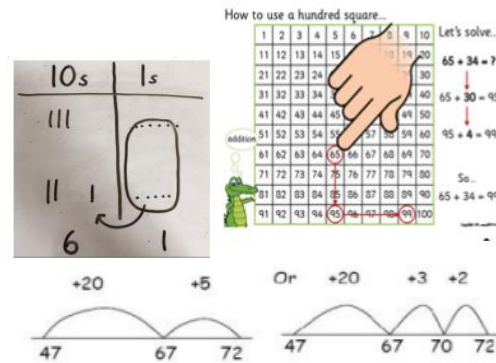
*Pupils should be able to apply known one-digit additive facts:

4	+	3	=	7
so 40	+	30	=	70
45	+	30	=	75

Adding two 2-digit numbers



Using a Hundred Square:



$$\begin{array}{r} 26 \\ 20 \end{array} + \begin{array}{r} 37 \\ 30 \end{array} = 63$$

$$\begin{array}{r} 20 + 30 = 50 \\ 6 + 7 = 13 \\ 50 + 13 = 63 \end{array}$$

$$\begin{array}{r} 26 + 30 = 56 \\ 56 + 7 = 63 \end{array}$$

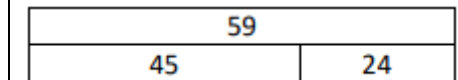
*Recording addition in columns supports place value and prepares for formal written methods with larger numbers.

$$\begin{array}{r} 40 + 7 \\ 30 + 5 \\ \hline 70 + 12 \end{array}$$

$$\begin{array}{r} 64 \\ + 17 \\ \hline 11 \\ + 70 \\ \hline 81 \end{array}$$

Use continuous bars, with increasing proportionality:

e.g. $45 + 24$



MENTALSTRATEGIES:

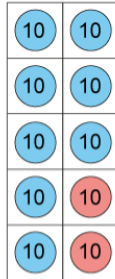
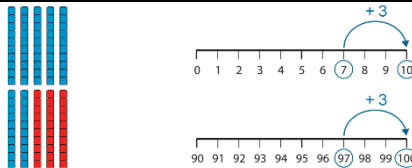
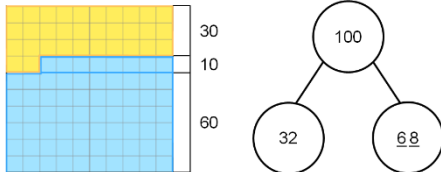
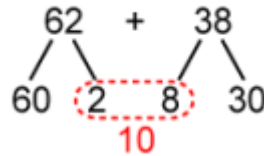
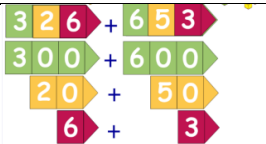
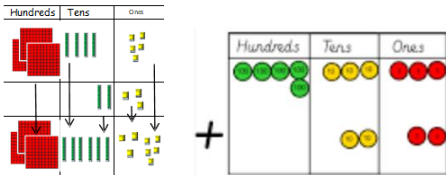
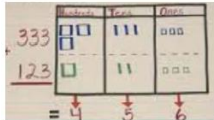
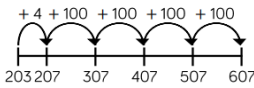
- Know that addition is the inverse of subtraction
- Add numbers mentally, including: a 2-digit number and ones, a multiple of 10 to a 2-digit number, two 2-digit numbers, three 1-digit numbers
- Use knowledge of inverse to check calculations and solve missing number problems
- Use knowledge of number bonds to 10 to calculate numbers bonds to 100
- Count on in tens from any given number (e.g. 19- 29 - 39 -49 etc)

Year 3 – Addition

Vocabulary: Pupils should use unitising language to describe within-column calculations : “3 ones plus 5 ones is equal to 8 ones.” “4 tens plus 2 tens is equal to 6 tens.”
Pupils should learn and use the correct names for the terms in addition and subtraction equations and understand addition is commutative:
Addend + addend = sum

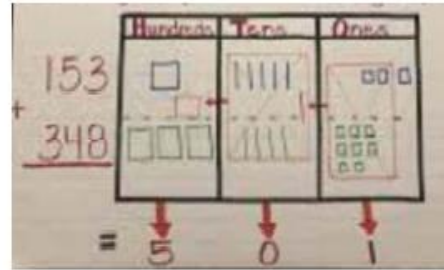
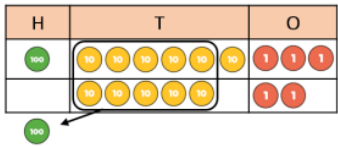
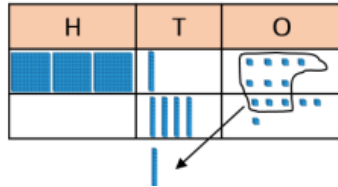
sum	
addend	addend

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-3-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/> , https://www.ncetm.org.uk/media/oagfcvjq/mastery_assessment_y3.pdf , <https://whiterosemaths.com/resources?year=year-3>

Method:	Concrete:	Pictorial:	Abstract:								
Calculating complements to 100	Scaling with tens frames: 	 <p>First make 10, then work out the additional number of tens needed:</p> $100 = 32 + \underline{68}$ 	<table border="1"><tr><td colspan="2">10</td></tr><tr><td>7</td><td>3</td></tr></table> $7 + 3 = 10$ <table border="1"><tr><td colspan="2">10 tens</td></tr><tr><td>7 tens</td><td>3 tens</td></tr></table> $97 + 3 = 100$ 	10		7	3	10 tens		7 tens	3 tens
10											
7	3										
10 tens											
7 tens	3 tens										
Add numbers with up to 3-digits, using formal written methods of columnar addition (no regrouping)	 	<p>*Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding.</p>  	$\begin{array}{r} 223 \\ + 114 \\ \hline 337 \end{array}$ <table border="1"><tr><td colspan="2">607</td></tr><tr><td>203</td><td>404</td></tr></table>	607		203	404				
607											
203	404										

Add numbers with up to 3-digits, using formal written methods of columnar addition (regrouping)

*Regrouping and exchange build on pupils' understanding that 10 ones is equivalent to 1 ten, and that 10 tens is equivalent to 1 hundred. Base 10/counters can be used to model the calculations, and to draw attention to the regrouping/exchange.



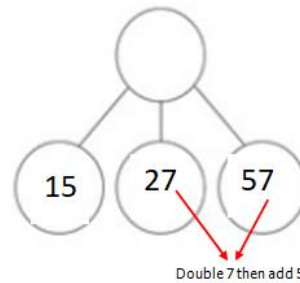
	3	1	7
+		4	6
	3	6	3
			1

To solve calculations with more than 2 addends.

*Discuss concept of commutative properties of addition



- Range of pictorial strategies available as above eg. Tens frames, place value grids, part-part whole, bar models.



$$\begin{array}{r}
 15 \\
 57 \\
 + 27 \\
 \hline
 99 \\
 1
 \end{array}$$

double

$$\begin{array}{r}
 416 \\
 223 \\
 + 184 \\
 \hline
 823 \\
 11
 \end{array}$$

make 10 make 10

MENTAL STRATEGIES:

- Know number pairs that total 1000 (multiples of 100)
- Calculate 10 or 100 more than any given number
- Add numbers mentally, including: a 3-digit number and single digit number, a 3-digit number and multiples of 10, a 3-digit number and multiples of 100
- Estimate the answer to a calculation and use inverse operations to check answers

Year 4 – Addition

Vocabulary: make connections between known facts and related calculations: “8 plus 6 is equal to 14, so 8 hundreds plus 6 hundreds is equal to 14 hundreds.” “14 hundred is equal to 1,400.”

Pupils should learn and use the correct names for the terms in addition and subtraction equations and understand addition is commutative:

Addend + addend = sum

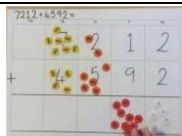
sum	
addend	addend

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-4-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/> , https://www.ncetm.org.uk/media/x45na0cs/mastery_assessment_y4.pdf , <https://whiterosemaths.com/resources?year=year-4>

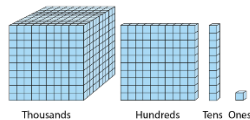
Method:

Using formal written methods of columnar addition where appropriate add numbers with up to 4 digits with regrouping.

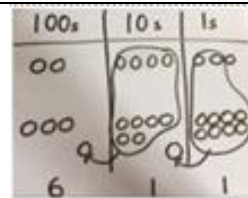
Concrete:



*Ideally children should move on to using counters to support understanding of unitising but base 10 can still be used if relative size understanding is still needed.



Pictorial:



Th	H	T	O
●●●●	●●●●●●	●●●●●●	●●●●●●
●●●●	●●●●●●	●●●●●●	●●●●●●
●●●●	●●●●●●	●●●●●●	●●●●●●

Abstract:

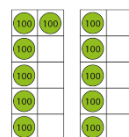
	Th	H	T	O
	2	1	7	6
+	3	4	5	8
	5	6	3	4

	Th	H	T	O
	4	—	6	—
+	2	5	—	1
	—	7	8	9

Add 2 or more numbers using columnar addition, including calculations whose addends have different numbers of digits.

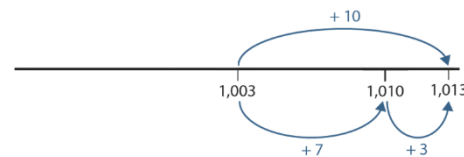
*Concrete resources such as place-value counters, partitioning diagrams and tens-frames can be used to help pupils understand calculation strategies and make connections between known facts and related calculations.

$$600 + 500 = 1,100$$



As above.

$$1,003 + 10 = 1,113$$



Pupils should add the digits within a column in the most efficient order

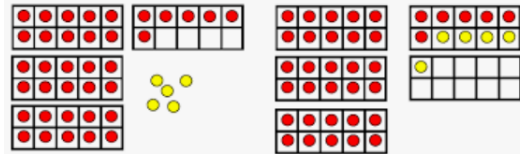
$$\begin{array}{r} 1,649 \\ 3,104 \\ + 516 \\ \hline 5,269 \\ \hline \end{array}$$

*beginning by making 10 in the ones column then making double-6 in the hundreds column

1,185	405
-------	-----

Use inverse operations to check answers to a calculation

*Concrete resources such as place-value counters, partitioning diagrams and tens-frames can be used to help show relationship between addition and subtraction facts by physically removing and regrouping amounts.



Eg. Tens frame above can show both addition and subtraction facts.

Show the following calculations using place value counters:

Thousands	Hundreds	Tens	Ones
1000	100 100 100 100	10 10	1
1000 1000		10 10 10	1 1 1 1 1 1 1 1

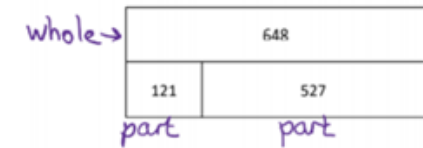
$$\begin{array}{r} 1421 \\ 2037 \\ \hline 3458 \end{array}$$

$$\begin{array}{r} 3458 \\ 2037 \\ \hline 1421 \end{array}$$

$$\begin{array}{l} 527 + 121 = 648 \\ 121 + 527 = 648 \\ 648 - 121 = 527 \\ 648 - 527 = 121 \end{array}$$

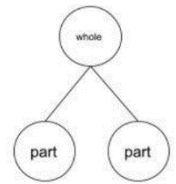
527 - 121 = 648
This would NOT be a correct sentence because 527 - 121 would equal 406.

*Use of column subtraction can help check answers.



Part + Part = Whole

Whole - Part = Part



MENTALSTRATEGIES:

- Add numbers mentally, including: a four digit number and multiples of one thousand
- Use knowledge of doubles to derive related facts (e.g $15 + 16 = 31$ because $15 + 15 = 30$ and $30 + 1 = 31$)
- Know number pairs that total 1000 (multiples of 10)
- Estimate the answer to a calculation and use inverse operations to check answers

Year 5 – Addition

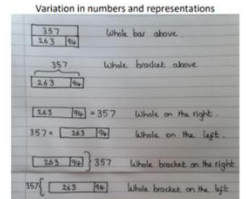
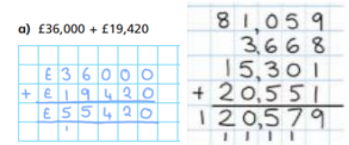
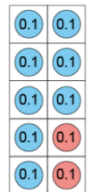
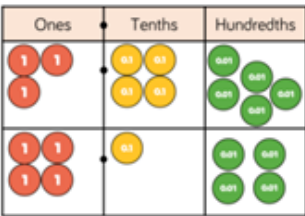
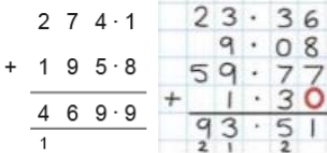
Vocabulary: make connections between known facts and related calculations: “8 plus 6 is equal to 14, so 8 tenths plus 6 tenths is equal to 14 tenths.” “14 tenths is equal to 1 one and 4 tenths.”

Pupils should learn and use the correct names for the terms in addition and subtraction equations and understand addition is commutative:

Addend + addend = sum

sum	
addend	addend

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-5-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/> , https://www.ncetm.org.uk/media/lp0o2lqv/mastery_assessment_y5.pdf , <https://whiterosemaths.com/resources?year=year-5>

Method:	Concrete:	Pictorial:	Abstract:
Children will add numbers with more than 4-digits using the formal written method of column addition in a variety of contexts	<p>*Concrete resources such as place-value counters, partitioning diagrams and tens-frames can be used to help pupils understand calculation strategies and make connections between known facts and related calculations. However, pupils should not rely on such representations for calculating. Pupils should instead be able to calculate by verbalising the relationship eg.</p> <div> <p>Language focus</p> <p>“8 plus 6 is equal to 14, so 8 tenths plus 6 tenths is equal to 14 tenths.”</p> <p>“14 tenths is equal to 1 one and 4 tenths.”</p> </div>	<p>Children know and understand the variation in representing addition using bar modelling:</p>  <p>“Whole below” is less conventional though children should understand that it is not incorrect.</p>	<p>a) £36,000 + £19,420</p>  <p>Children should make a transition from discrete to continuous bar models for most areas of maths and be able to draw these independently and accurately with increasing levels of proportionality.</p>
Children will add numbers with up to 2 decimal places.	<p>Scaling with 10's frames and decimal counters.</p> 		 <p>Calculate numbers with increasing complexity including use of zero as place holder when addends have different numbers of digits.</p>

MENTALSTRATEGIES:

- Add numbers mentally with increasingly large numbers (e.g $10,162 + 2,300 = 12,462$)
- Mentally add tenths (e.g $0.2 + 0.6 = 0.8$) and 1-digit whole numbers and tenths ($8 + 0.3 = 8.3$)
- Use number bonds to 100 knowledge to calculate complements to one using hundredths (e.g $0.83 + 0.17 = 1$)
- Use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy

Year 6 – Addition

Vocabulary: Children know that the relationship between 2 numbers can be expressed additively. In year 6, pupils should learn the compensation property of addition: “If one addend is increased and the other is decreased by the same amount, the sum stays the same.”

Pupils should learn and use the correct names for the terms in addition and subtraction equations and understand addition is commutative:

Addend + addend = sum

sum	
addend	addend

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-6-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/> , https://www.ncetm.org.uk/media/uitj1x5q/mastery_assessment_y6.pdf , <https://whiterosemaths.com/resources?year=year-6>

Method:

Children should continue to practise adding whole numbers with increasing difficulty, and numbers with different amounts of decimal places, using columnar addition to solve problems in a range of contexts.

Concrete:

*Concrete resources such as place-value counters, partitioning diagrams and tens-frames can be used to help pupils understand calculation strategies and make connections between known facts and related calculations. However, pupils should not rely on such representations for calculating. Pupils should instead be able to calculate by verbalising the relationship

Millions			Thousands			Ones		
100s	10s	1s	100s	10s	1s	100s	10s	1s
		●	●	●				

Pictorial:

Gentengo charts support understanding of scaling numbers:

10,000,000	20,000,000	30,000,000	40,000,000	50,000,000	60,000,000	70,000,000	80,000,000	90,000,000
1,000,000	2,000,000	3,000,000	4,000,000	5,000,000	6,000,000	7,000,000	8,000,000	9,000,000
100,000	200,000	300,000	400,000	500,000	600,000	700,000	800,000	900,000
10,000	20,000	30,000	40,000	50,000	60,000	70,000	80,000	90,000
1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9
0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09

Abstract:

?
2,354
750
1,500

2	3	5	4
7	5	0	
+	1	5	0
	4	6	4
	1		

23.361 + 9.08 + 59.77 + 1.3 = 93.511

23.361
9.080
59.770
1.300
93.511

Zero used as a place value holder.

– 233,233 = 322,322

3	2	2	3	2	2
+	2	3	3	2	3
	5	5	5	5	5

555,555




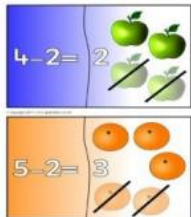
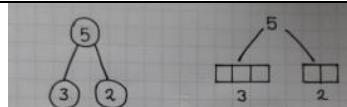

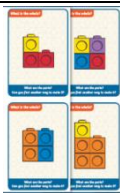
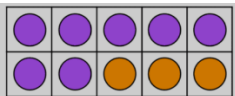

MENTAL STRATEGIES:

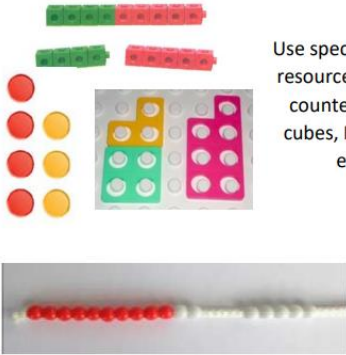
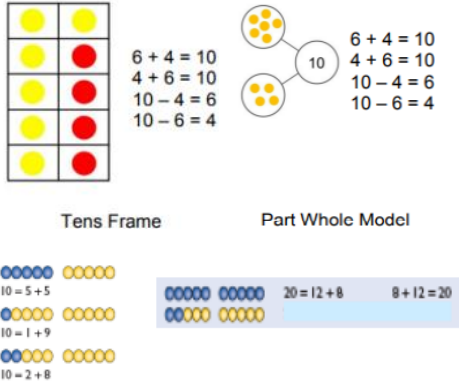
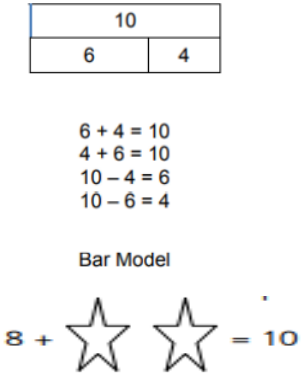
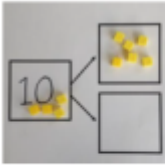
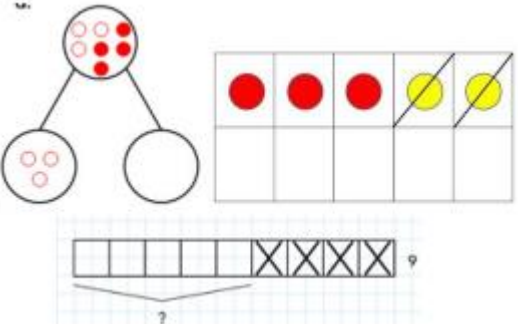

- Add numbers mentally with increasingly large numbers (e.g. 10,162 + 2,300 = 12,462)
- Add decimal numbers mentally (up to 2 decimal places)
- Use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy.

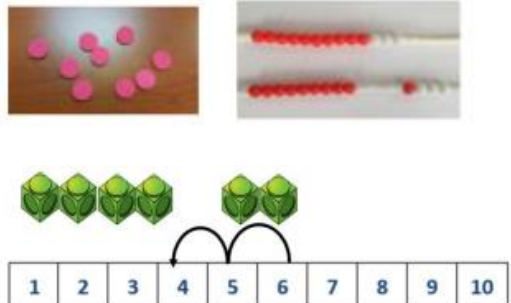
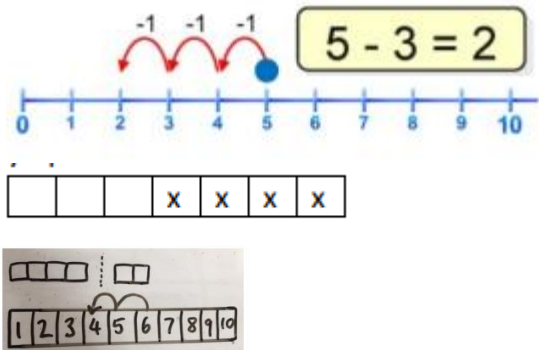
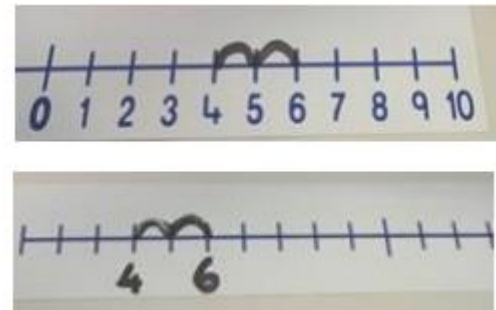

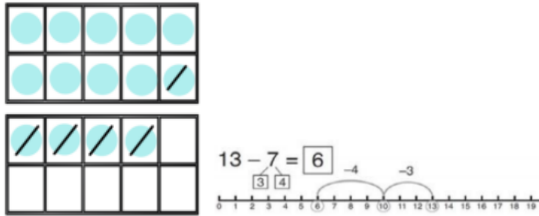
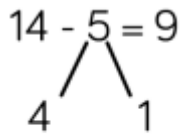
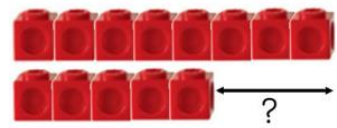
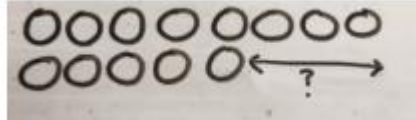
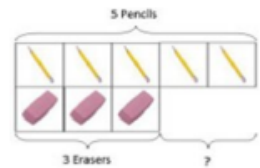
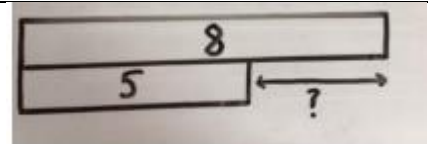


Subtraction Guidance



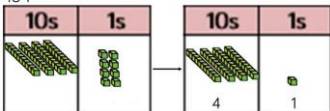
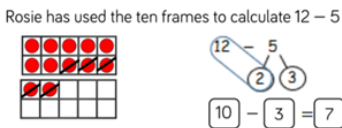
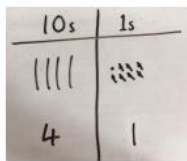
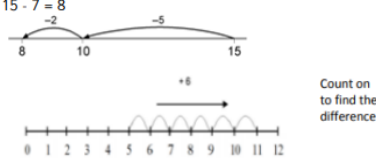
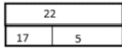
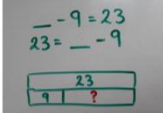
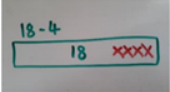


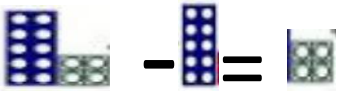
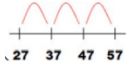
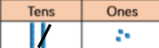
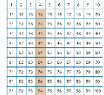

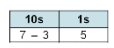

EYFS – Subtraction			
Vocabulary: fives frame, tens frame, whole, part, take away, subtract, bigger, smaller, equal			
Helpful Videos/Resources: https://www.ncetm.org.uk/classroom-resources/ey-numberblocks-support-materials/			
Method:	Concrete:	Pictorial:	Abstract:
Counting backwards from 5	Child initiated games indoors and outdoors such as acting out counting songs and running races (children shouting "5,4,3,2,1,0 - GO!").		Relationships between pictures and objects as numerals  1 2 3
Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 including subtraction facts	Children to understand that subtraction is taking away objects practically. Equals means we find out how many we have got left. 		 Using both of these representations for number bonds will ensure children are provided with variation in their representations and also begin to build foundations for independently drawing these in Year 1. A large emphasis is placed on the part and whole vocabulary and links between addition and subtract facts.
Have a deep understanding of number to 10, including the composition of each number	  Represent numbers in different ways using numicon/other resources eg. Multilink. Make links to subtraction facts to build on addition facts.	Use of tens frames to sort objects/counters to take off as well as add on. 	Relationships between pictures and objects as numerals and words – counting backwards as well as forwards. 
MENTAL STRATEGIES: - Verbally count beyond 20			

Year 1 – Subtraction			
Vocabulary: equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how much less is...			
Helpful Videos/Resources: https://www.ncetm.org.uk/classroom-resources/cp-year-1-curriculum-map/ , https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/ , https://www.ncetm.org.uk/media/qjpct24/mastery_assessment_v1.pdf , https://whiterosemaths.com/resources?year=year-1			
Method:	Concrete:	Pictorial:	Abstract:
Represent and use number bonds and related subtraction facts within 20	 <p>Use specific maths resources such as counters, snap cubes, Numicon etc.</p>	 <p>Tens Frame</p> <p>Part Whole Model</p> <p>10 = 5 + 5 10 = 1 + 9 10 = 2 + 8</p> <p>20 = 12 + 8 8 + 12 = 20</p>	 <p>10</p> <p>6 4</p> <p>6 + 4 = 10 4 + 6 = 10 10 - 4 = 6 10 - 6 = 4</p> <p>Bar Model</p> <p>8 + 2 = 10</p>
Links to part whole model and addition – finding a part if you know the whole.	 <p>Link to addition. Use PPW model to model the inverse.</p> <p>If 10 is the whole and 6 is one of the parts, what is the other part?</p> <p>10 - 6 = 4</p> <p>Use cubes to partition numbers into groups or in a bar. (Some children may still need to use real objects)</p>	 <p>The Bar Model will be continued from EYFS as a method to support problem solving involving addition, continuing with the concrete representations and moving onto using pictorial representations of objects.</p>	A focus on symbols and numbers to form a calculation and fact families. 

<p>Starting at the bigger number and counting back</p>	<p>Use counters, move them away from the group counting backwards as you go.</p> 		
<p>Subtracting to make 10</p>	<p>$14 - 9 =$</p>  <p>Make 14 on the ten frame. Take away the four first to make 10 and then take away one more so you have taken away 5. You are left with the answer of 9.</p>		<p>$14 - 5 = 9$</p>  <p>$14 - 4 = 10$ $10 - 1 = 9$</p>
<p>Finding the difference</p>	<p>Use concrete apparatus in linear fashion to compare the sizes. Identify the gap representing the difference. Discuss how many more / how many less.</p>  <p>Can use cubes, numicon, counters or objects.</p>	 	

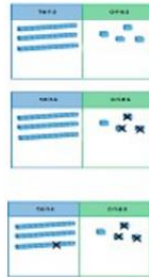
MENTAL STRATEGIES:

- Memorise and reason with number bonds to 10 and 20 in several forms (for example, $9 + 7 = 16$; $16 - 7 = 9$; $7 = 16 - 9$)
- Realise the effect of adding or subtracting zero
- Combine and increase numbers, counting forwards and backwards

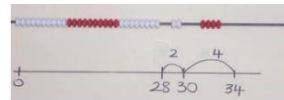
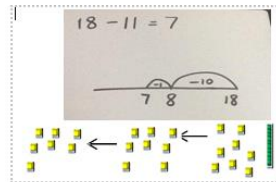
Year 2 – Subtraction			
Vocabulary: subtract, minus, leave, how many are left/left over?, how many less is... than...?, how much fewer is...?, difference between, half, halve, equals, sign, is the same as, partition, inverse, count on, count back, one less, ten less...one hundred less.			
Helpful Videos/Resources: https://www.ncetm.org.uk/classroom-resources/cp-year-2-curriculum-map/ , https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/ , https://www.ncetm.org.uk/media/dnbt14/mastery_assessment_yr2.pdf , https://whiterosemaths.com/resources?year=year-2			
Method:	Concrete:	Pictorial	Abstract:
Subtracting a 2-digit number and ones *Regrouping and exchange build on pupils' understanding that 10 ones is equivalent to 1 ten. Base 10/tens frames/Numicon can be used to model the calculations, and to draw attention to the regrouping/exchange.	Continue to develop understanding of partitioning and place value using base 10 and place value grids: $48 - 7 = 41$  Use 10's frames, numicon and base 10 to build on knowledge of regrouping/making 10: Rosie has used the ten frames to calculate $12 - 5$ 	Draw base 10 image and cross out to show: $48 - 7 = 41$  Steps in subtraction can be recorded on a number line. The steps often bridge through a multiple of 10. $15 - 7 = 8$  Count on to find the difference.	Explore related facts $17 + 5 = 22$ $5 + 17 = 22$ $22 - 17 = 5$ $22 - 5 = 17$   Draw on a continuous model and count back  *Pupils do not need to learn formal written methods for addition and subtraction in year 2, but column addition and column subtraction could be used as an alternative way to record two-digit calculations at this stage. 
Subtracting a 2-digit number and multiples of 10	 $25 - 10 = 15$  $14 - 10 = 4$	$57 - 30 = 27$ $23 - 3 = 13$   Base 10 may be used above the number line initially.   *Ensure understanding that the ones digit does not change with all representations	$75 - 30 = 45$   *Pupils should be able to apply known one-digit additive facts: $7 - 3 = 4$ $70 - 30 = 40$ $75 - 30 = 45$

Subtracting two 2-digit numbers

$$34 - 13 = 21$$



Use Dienes to show how to partition the number when subtracting without regrouping.



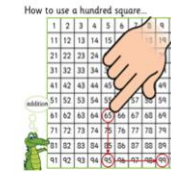
$$34 - 28$$

Use a bead bar or bead strings to model counting to next ten and the rest.

Children draw representations of Dienes and cross off.

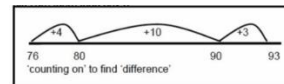
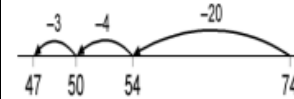
$$43 - 21 = 22$$

Using a Hundred Square:



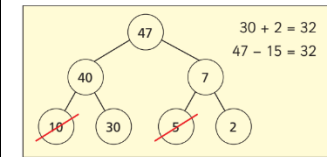
Use base 10 to support subtracting on a numberline:

$$74 - 27 = 47 \text{ worked by counting back:}$$



Use a number line to count on to next ten and then the rest.

Jack is working out $47 - 15$

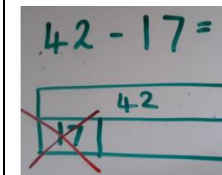


$$\begin{aligned} 74 - 27 &= \\ 74 - 20 &= 54 \\ 54 - 4 &= 50 \\ 50 - 3 &= 47 \end{aligned}$$

*Recording subtraction in columns supports place value and prepares for formal written methods with larger numbers.

$$\begin{array}{r} 40 + 8 \\ 10 + 6 \\ \hline 30 + 2 \end{array}$$

Use continuous bars, with increasing proportionality:



MENTALSTRATEGIES:

- Know that addition is the inverse of subtraction
- Subtract numbers mentally, including: a 2-digit number and ones, a multiple of 10 to a 2-digit number, two 2-digit numbers
- Use knowledge of inverse to check calculations and solve missing number problems
- Use knowledge of number bonds to 10 to calculate numbers bonds to 100
- Count back in tens from any given number (e.g. 19 - 29 - 39 - 49 etc)

Year 3 – Subtraction

Vocabulary: Pupils should use unitising language to describe within-column calculations : “5 ones minus 3 ones is equal to 2 ones.” “6 tens minus 2 tens is equal to 4 tens.”
Pupils should learn and use the correct names for the terms in addition and subtraction equations:
“If we swap the values of the subtrahend and difference, the minuend remains the same.”

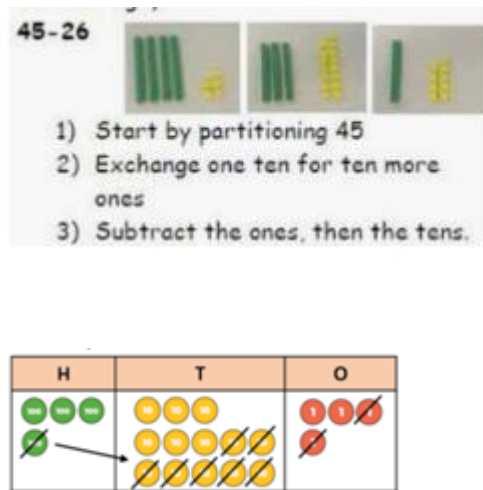
minuend		minuend	
subtrahend	difference	difference	subtrahend

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-3-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/> , https://www.ncetm.org.uk/media/oaqfcvjg/mastery_assessment_y3.pdf , <https://whiterosemaths.com/resources?year=year-3>

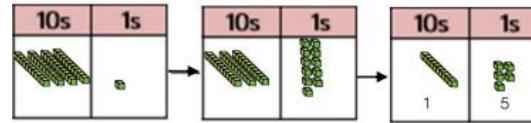
Method:	Concrete:	Pictorial:	Abstract:																												
Calculating complements to 100	Scaling with tens frames: 	<p>First make 10, then work out the additional number of tens needed:</p>	Use knowledge of fact families and complements to 100 to solve increasingly complex problems. <table border="1"><tr><td colspan="2">10</td></tr><tr><td>7</td><td>3</td></tr></table> $10 - 7 = 3$ $10 - 3 = 7$ <table border="1"><tr><td colspan="2">10 tens</td></tr><tr><td>7 tens</td><td>3 tens</td></tr></table> $70 + \underline{\quad} = 100$ $\underline{\quad} + 30 = 100$	10		7	3	10 tens		7 tens	3 tens																				
10																															
7	3																														
10 tens																															
7 tens	3 tens																														
Subtract numbers with up to 3-digits, using formal written methods of columnar addition (no regrouping)	<p>Use base 10 or numicon to model</p>	<table border="1"><tr><th></th><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td>3</td><td>5</td><td>8</td></tr><tr><td>-</td><td>2</td><td>2</td><td>6</td></tr><tr><td></td><td></td><td></td><td></td></tr></table> <p>*Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding.</p>		H	T	O		3	5	8	-	2	2	6					<table border="1"><tr><td></td><td>6</td><td>★</td><td>8</td></tr><tr><td>-</td><td>★</td><td>△</td><td>△</td></tr><tr><td></td><td>●</td><td>1</td><td>5</td></tr></table>		6	★	8	-	★	△	△		●	1	5
	H	T	O																												
	3	5	8																												
-	2	2	6																												
	6	★	8																												
-	★	△	△																												
	●	1	5																												

Subtract numbers with up to 3-digits, using formal written methods of columnar addition (one exchange)

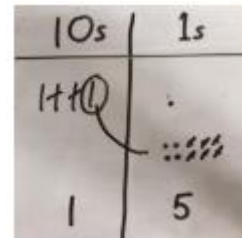
*Regrouping and exchange build on pupils' understanding that 10 ones is equivalent to 1 ten, and that 10 tens is equivalent to 1 hundred. Base 10/counters can be used to model the calculations, and to draw attention to the regrouping/exchange.



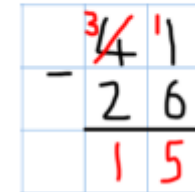
41 - 26



Begin to record by drawing and showing the exchange.

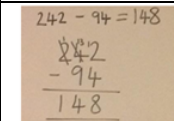
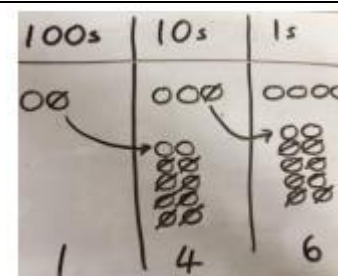
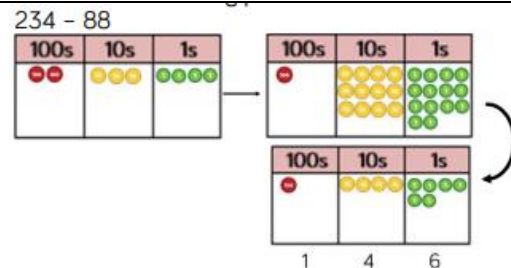


Formal column method. Children must understand that when they have exchanged the 10 they still have 41 because $41 = 30 + 11$.

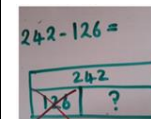


Subtract numbers with up to 3-digits, using formal written methods of columnar addition (more than one exchange)

*Regrouping and exchange build on pupils' understanding that 10 ones is equivalent to 1 ten, and that 10 tens is equivalent to 1 hundred. Base 10/counters can be used to model the calculations, and to draw attention to the regrouping/exchange.



Use continuous bars, with increasing proportionality:



MENTAL STRATEGIES:

- Know number pairs that total 1000 (multiples of 100)
- Calculate 10 or 100 more than any given number
- Subtract numbers mentally, including: a 3-digit number and single digit number, a 3-digit number and multiples of 10, a 3-digit number and multiples of 100
- Estimate the answer to a calculation and use inverse operations to check answers

Year 4 – Subtraction


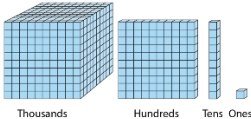
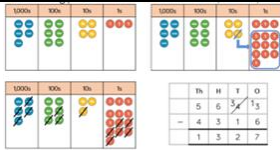
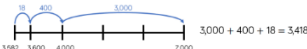
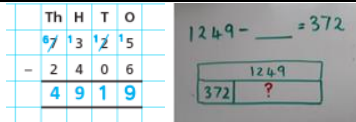
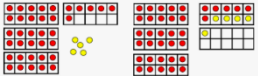
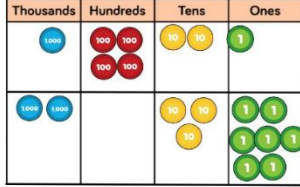
Vocabulary: Vocabulary: Pupils should use unitising language to describe within-column calculations : “5 ones minus 3 ones is equal to 2 ones.” “6 hundreds minus 2 hundreds is equal to 4 hundreds.”

Pupils should learn and use the correct names for the terms in addition and subtraction equations:

“If we swap the values of the subtrahend and difference, the minuend remains the same.”

minuend		minuend	
subtrahend	difference	difference	subtrahend

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-4-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/> , https://www.ncetm.org.uk/media/x45na0cs/mastery_assessment_y4.pdf , <https://whiterosemaths.com/resources?year=year-4>

Method:	Concrete:	Pictorial:	Abstract:
Using formal written methods of columnar subtraction where appropriate to subtract numbers with up to 4 digits with exchanging.	 <p>*Ideally children should move on to using counters to support understanding of unitising but base 10 can still be used if relative size understanding is still needed.</p>  <p>Thousands Hundreds Tens Ones</p>	 <p>*Use columnar subtraction where appropriate - Finding the difference on a number line may be more appropriate when minuend is multiple of 1000:</p> <p>Eg. 7000 - 3418</p>  <p>3,000 + 400 + 18 = 3,418</p>	 <p>Pupils should make sensible decisions about how and when to use columnar subtraction. They may transform to an equivalent calculation before using column subtraction, avoiding the need to exchange through zeroes:</p> $\begin{array}{r} 7,000 \\ - 2,648 \\ \hline \end{array} \xrightarrow{-1} \begin{array}{r} 6,999 \\ - 2,647 \\ \hline \end{array}$ <p>527 + 121 = 648 121 + 527 = 648 648 - 121 = 527 648 - 527 = 121</p> <p>527 - 121 = 648 This would NOT be a correct sentence because 527 - 121 would equal 406.</p> <p>*Use of column subtraction can help check answers.</p>
Use inverse operations to check answers to a calculation	<p>*Concrete resources such as place-value counters, partitioning diagrams and tens-frames can be used to help show relationship between addition and subtraction facts by physically removing and regrouping amounts.</p>  <p>Eg. Tens frame above can show both addition and subtraction facts.</p>	<p>Show the following calculations using place value counters.</p>  <p>1421 2037 3458</p> <p>3458 2037 1421</p>	

MENTALSTRATEGIES:

- Subtract numbers mentally, including: a four digit number and multiples of one thousand
- Use knowledge of doubles to derive related facts (e.g 15 + 16 = 31 because 15 + 15 = 30 and 30 + 1 = 31)
- Know number pairs that total 1000 (multiples of 10)
- Estimate the answer to a calculation and use inverse operations to check answers

Year 5 – Subtraction

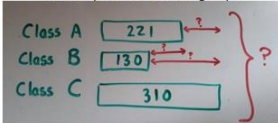
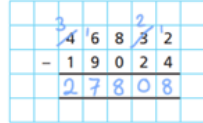

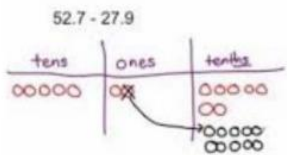

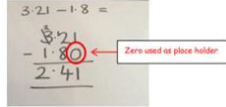
Vocabulary: make connections between known facts and related calculations: “8 plus 6 is equal to 14, so 8 tenths plus 6 tenths is equal to 14 tenths.” “14 tenths is equal to 1 one and 4 tenths.”

Pupils should learn and use the correct names for the terms in addition and subtraction equations:

“If we swap the values of the subtrahend and difference, the minuend remains the same.”

minuend		minuend	
subtrahend	difference	difference	subtrahend

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-5-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/> , https://www.ncetm.org.uk/media/lp0o2lqv/mastery_assessment_y5.pdf , <https://whiterosemaths.com/resources?year=year-5>

Method:	Concrete:	Pictorial:	Abstract:
Children will subtract numbers with more than 4-digits using the formal written method of column subtraction in a variety of contexts including finding the difference	*Concrete resources such as place-value counters, partitioning diagrams and tens-frames can be used to help pupils understand calculation strategies and make connections between known facts and related calculations. However, pupils should not rely on such representations for calculating. Pupils should instead be able to calculate by verbalising the relationship.	Children know and understand the variation in representing subtraction using bar modelling: Use comparison continuous models to find the difference, find the whole with numbers ≥ 3 digits. Also compare more than 2 groups. 	 Children should make a transition from discrete to continuous bar models for most areas of maths and be able to draw these independently and accurately with increasing levels of proportionality.
Children will subtract numbers with up to 2 decimal places.		 When confident, children can find their own way to record the exchange/regrouping	 Calculate numbers with increasing complexity including use of zero as place holder when subtrahends have different numbers of digits. 

MENTAL STRATEGIES:

- Subtract numbers mentally with increasingly large numbers (e.g $10,162 - 2,100 = 8,062$)
- Mentally subtract tenths (e.g $0.8 - 0.6 = 0.2$) and 1-digit whole numbers and tenths ($8 - 0.3 = 7.7$)
- Use number bonds to 100 knowledge to calculate complements to one using hundredths (e.g $0.83 + 0.17 = 1$)
- Use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy

Year 6 – Subtraction

Vocabulary: make connections between known facts and related calculations: “8 plus 6 is equal to 14, so 8 tenths plus 6 tenths is equal to 14 tenths.” “14 tenths is equal to 1 one and 4 tenths.”

Pupils should learn and use the correct names for the terms in addition and subtraction equations:

“If we swap the values of the subtrahend and difference, the minuend remains the same.”

minuend		minuend	
subtrahend	difference	difference	subtrahend

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-6-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/> , https://www.ncetm.org.uk/media/uitj1x5q/mastery_assessment_y6.pdf , <https://whiterosemaths.com/resources?year=year-6>

Method:

Children should continue to practise subtracting whole numbers with increasing difficulty, and numbers with different amounts of decimal places, using columnar subtraction to solve problems in a range of contexts.

Concrete:

*Concrete resources such as place-value counters, partitioning diagrams and tens-frames can be used to help pupils understand calculation strategies and make connections between known facts and related calculations. However, pupils should not rely on such representations for calculating. Pupils should instead be able to calculate by verbalising the relationship

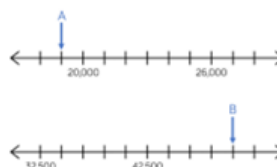
Millions			Thousands			Ones		
100s	10s	1s	100s	10s	1s	100s	10s	1s
		●	●	●				

Pictorial:

Gentengo charts support understanding of scaling numbers:

10,000,000	20,000,000	30,000,000	40,000,000	50,000,000	60,000,000	70,000,000	80,000,000	90,000,000
1,000,000	2,000,000	3,000,000	4,000,000	5,000,000	6,000,000	7,000,000	8,000,000	9,000,000
100,000	200,000	300,000	400,000	500,000	600,000	700,000	800,000	900,000
10,000	20,000	30,000	40,000	50,000	60,000	70,000	80,000	90,000
1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9
0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09

Find the difference between A and B.



Abstract:

$$\begin{array}{r}
 63719 - 2352 - 175 = \\
 2352 \\
 + 175 \\
 \hline
 2527 \\
 63719 \\
 - 2527 \\
 \hline
 61192
 \end{array}$$

$$\begin{array}{r}
 7.35 - 2.1 - 1.675 \\
 1.675 \\
 + 2.1 \\
 \hline
 3.775 \\
 7.35 \\
 - 3.775 \\
 \hline
 3.575
 \end{array}$$

Zero used as place holder

Pupils should make sensible decisions about how and when to use columnar methods. For example, when subtracting a decimal fraction from a whole number, pupils may be able to use their knowledge of complements, avoiding the need to exchange through zeroes. For example, to calculate $8 - 4.85$ pupils should be able to work out that the decimal complement to 5 from 4.85 is 0.15, and that the total difference is therefore 3.15.


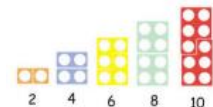
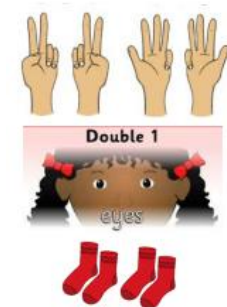
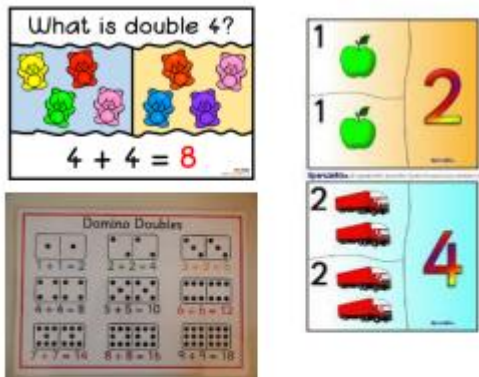
MENTALSTRATEGIES:



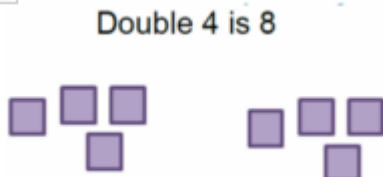
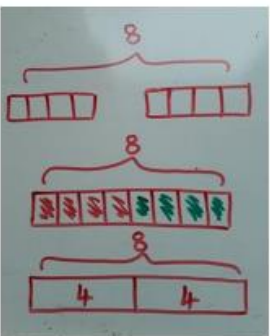
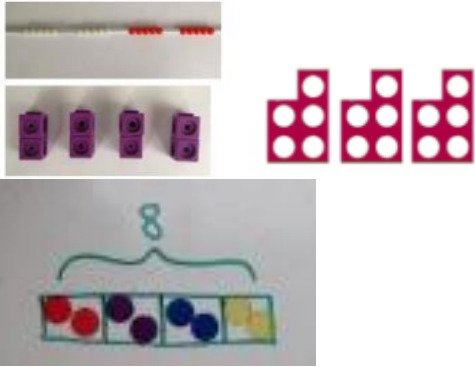
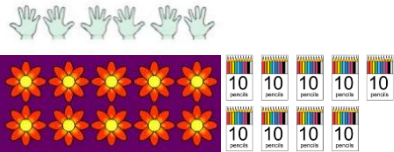
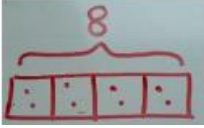
- Subtract numbers mentally with increasingly large numbers
- Subtract decimal numbers mentally (up to 2 decimal places)
- Use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy.

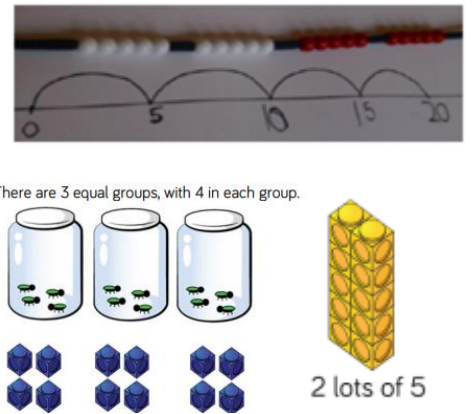
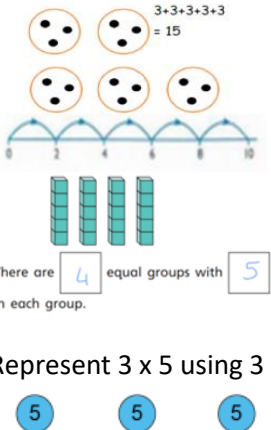
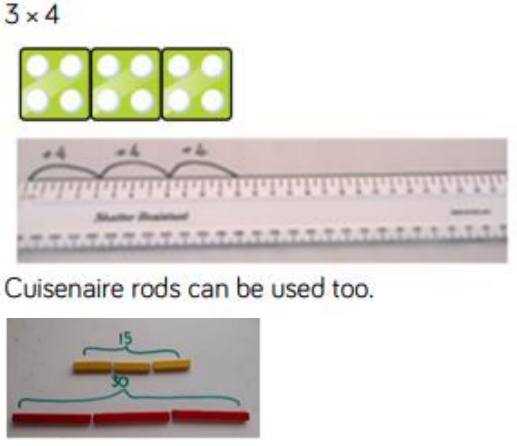
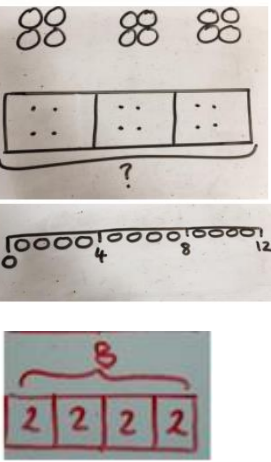


Multiplication Guidance



EYFS – Multiplication								
Vocabulary: double, equal, groups, altogether, add								
Helpful Videos/Resources: https://www.ncetm.org.uk/classroom-resources/ey-numberblocks-support-materials/								
Method:	Concrete:	Pictorial:	Abstract:					
Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 and some number bonds to 10, including double facts.	<div></div> <div></div> <div></div> <div>Counting and other maths resources for children to make 2 equal groups.</div> <div>Physical and real life examples that encourage children to see concept of doubling as adding two equal groups.</div>	<div></div> <div>Pictures and icons that encourage children to see concept of doubling as adding two equal groups.</div>	<div><table><tr><td>1+1=</td></tr><tr><td>2+2=</td></tr><tr><td>3+3=</td></tr><tr><td>4+4=</td></tr><tr><td>5+5=</td></tr></table></div> <div>Addition calculations to model adding two equal groups.</div>	1+1=	2+2=	3+3=	4+4=	5+5=
1+1=								
2+2=								
3+3=								
4+4=								
5+5=								
MENTAL STRATEGIES: - Verbally count beyond 20								

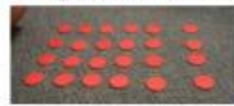
Year 1 – Multiplication			
Vocabulary: Groups of, lots of, times, array, altogether, multiply			
Helpful Videos/Resources: https://www.ncetm.org.uk/classroom-resources/cp-year-1-curriculum-map/ , https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/multiplication-and-division/ , https://www.ncetm.org.uk/media/qjpct24/mastery_assessment_y1.pdf , https://whiterosemaths.com/resources?year=year-1			
Method:	Concrete:	Pictorial:	Abstract:
Through grouping and sharing small quantities, pupils begin to understand doubling numbers and quantities	 <p>Use specific maths resources such as counters, snap cubes, Numicon etc.</p> 	 <p>Double 4 is 8</p>	
Count in multiples of 2s, 5s, 10s		<p>Use images and arrays to support recall of multiples through repeated addition and skip counting.</p>  	<p>2, 4, 6, 8, 10</p> <p>5, 10, 15, 20, 25, 30</p> <p>*Pupils do not need to be introduced to the words 'multiplication' and 'division' or to the multiplication and division symbols in year 1 and are not expected to solve calculations presented as written equations.</p>
MENTAL STRATEGIES: <ul style="list-style-type: none"> - count fluently, both forwards and backwards - sequencing in ones will extend to sequencing in multiples of 2, 5 and 10 - recite the odd number sequence, both forwards and backwards. 			

Year 2 – Multiplication			
Vocabulary: odd, even, twos, fives, tens, threes, lots of, groups of, once, twice, three times, five times, ten times, multiple of, times, multiply, multiply by, repeated addition, array, row, column, double.			
Helpful Videos/Resources: https://www.ncetm.org.uk/classroom-resources/cp-year-2-curriculum-map/ , https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/multiplication-and-division/ , https://www.ncetm.org.uk/media/dnbt14/mastery_assessment_yr2.pdf , https://whiterosemaths.com/resources?year=year-2			
Method:	Concrete:	Pictorial	Abstract:
Recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers	 <p>There are 3 equal groups, with 4 in each group.</p> <p>2 lots of 5</p>	 <p>3 + 3 + 3 + 3 + 3 = 15</p> <p>There are 4 equal groups with 5 in each group.</p> <p>Represent 3 x 5 using 3 five-value counters:</p>	Skip counting: Write sequences with multiples of numbers. 0, 2, 4, 6, 8, 10
Calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (×), division (÷) and equals (=) signs	 <p>3×4</p> <p>Cuisenaire rods can be used too.</p>		$3 \times 4 = 12$ $4 + 4 + 4 = 12$

Show that multiplication of two numbers can be done in any order (commutative)

Create arrays using counters and cubes and

Numicon.



Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.



$$2 \times 4 = 8$$

$$4 \times 2 = 8$$



$$2 \times 4 = 8$$

$$4 \times 2 = 8$$

$$5 \times 3 = 15$$

$$3 \times 5 = 15$$

e.g. 4×10 is 4 lots of 10

40			
10	10	10	10

4×10 is 10 lots of 4

40									
4	4	4	4	4	4	4	4	4	4

MENTALSTRATEGIES:

- Count forwards and backwards in multiples of 3.
- Know the 2, 5 and 10 times tables (in and out of order)
- Recognise odd and even numbers


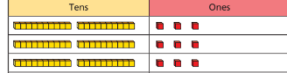
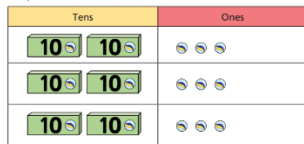
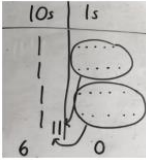

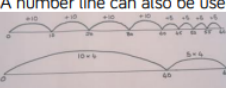
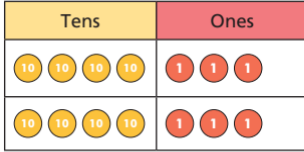
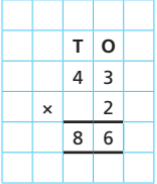

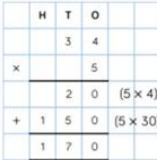
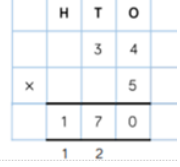
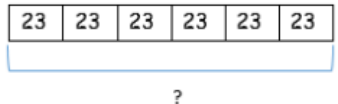
Year 3 – Multiplication

Vocabulary: “factor times factor is equal to product”, “The order of the factors does not affect the product.”

$$\begin{array}{c} \text{Factor} \quad 2 \times 5 = 10 \quad \text{Product} \\ \text{Factor} \end{array}$$

$$\begin{array}{r} 2 \\ \times 5 \\ \hline 10 \end{array} \quad \begin{array}{l} \text{Factor} \\ \text{Factor} \\ \text{Product} \end{array}$$

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-3-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/multiplication-and-division/> , https://www.ncetm.org.uk/media/oagfcvjq/mastery_assessment_y3.pdf , <https://whiterosemaths.com/resources?year=year-3>

Method:	Concrete:	Pictorial:	Abstract:
Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental methods	<p>4 x 15</p>  <p>23 x 3 =</p> 	<p>Ron, Eva and Mo each have 23 marbles.</p>  	<p>4 x 15</p>  <p>10 x 4 = 40 5 x 4 = 20 40 + 20 = 60</p> <p>A number line can also be used</p> 
Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, progressing to formal written methods	<p>Use manipulatives next to column method to introduce/support:</p>   <p>Numicon and base 10 can still be used to represent place value and relative size of amounts.</p>	<p>2 3</p> $\begin{array}{r} 3 \times \\ 9 \quad (3 \times 3) \\ 60 \quad (3 \times 20) \\ \hline 69 \end{array}$   <p>Pupils can use expanded to begin with to ensure place value is explicit and support with carrying but move onto compact method as soon as ready making links with previous work on column addition.</p>	<p>23</p> $\begin{array}{r} 23 \\ \times 3 \\ \hline 69 \end{array}$  

MENTAL STRATEGIES:

- Count forwards and backwards in multiples of 4, 8, 50 & 100
- Know the 3, 4 and 8 times tables (in and out of order)
- Connect the 2, 4 and 8 times tables through doubling
- Use knowledge of place value to calculate multiplication (e.g. $2 \times 2 = 4$, $2 \times 20 = 40$, $2 \times 200 = 400$)

Year 4 – multiplication







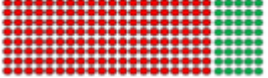

























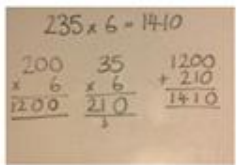
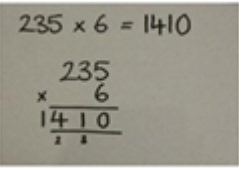















Vocabulary: “factor times factor is equal to product”, “The order of the factors does not affect the product.”

Pupils should be able reason in terms of unitising in hundreds, or in terms of scaling a factor by 100:
 “3 times 5 is equal to 15. 3 times 5 hundreds is equal to 15 hundreds. 15 hundreds is equal to 1,500.”
 “If I multiply one factor by 100, I must multiply the product by 100.”

$$\begin{array}{ccc} & 2 & \times 5 = 10 \\ \text{Factor} & & \text{Factor} & & \text{Product} \end{array}$$

$$\begin{array}{r} 2 \\ \times 5 \\ \hline 10 \end{array} \quad \begin{array}{l} \text{Factor} \\ \text{Factor} \\ \text{Product} \end{array}$$

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-4-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/multiplication-and-division/> , https://www.ncetm.org.uk/media/x45na0cs/mastery_assessment_y4.pdf , <https://whiterosemaths.com/resources?year=year-4>

Method:	Concrete:	Pictorial:	Abstract:																																
Multiply two-digit and three-digit numbers by a one-digit number using formal written layout	<div><table><tr><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></table><div>$25 \times 8 = 20 \times 8 + 5 \times 8$$= 160 + \square = \square$</div></div>	Tens	Ones							<div><table><tr><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr></table></div>	H	T	O										<div><div>$235 \times 6 = 1410$</div><div>$235 \times 6 = 1410$</div></div> <div>Irvin bought 6 bags of apples, each weighing 132kg.</div> <div><table><tr><td colspan="6">?</td></tr><tr><td>132</td><td>132</td><td>132</td><td>132</td><td>132</td><td>132</td></tr></table></div>	?						132	132	132	132	132	132
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MENTALSTRATEGIES:

- Recall multiplication and division facts for multiplication tables up to 12×12
- Use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1; dividing by 1; multiplying together three numbers
- Recognise and use factor pairs and commutativity in mental calculations
- Know that 10×5 is 10×10 then divide by 2 (e.g. $18 \times 5 = (18 \times 10) \div 2 = 90$)
- Know that 10×9 is 10×10 then subtract 10 (e.g. $18 \times 9 = (18 \times 10) - 18 = 162$)

Year 5 – Multiplication


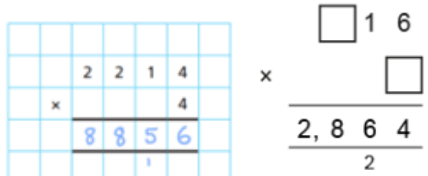
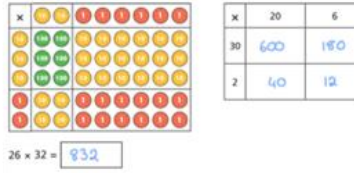
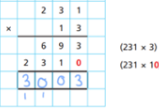
Vocabulary: “factor times factor is equal to product”, “The order of the factors does not affect the product.”

Pupils should be able reason in terms of unitising in hundreds, or in terms of scaling a factor by 100:
 “3 times 5 is equal to 15. 3 times 5 hundreds is equal to 15 hundreds. 15 hundreds is equal to 1,500.”
 “If I multiply one factor by 100, I must multiply the product by 100.”

$$\begin{array}{c} 2 \times 5 = 10 \\ \text{Factor} \quad \text{Factor} \quad \text{Product} \end{array}$$

$$\begin{array}{r} 2 \\ \times 5 \\ \hline 10 \end{array} \quad \begin{array}{l} \text{Factor} \\ \text{Factor} \\ \text{Product} \end{array}$$

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-5-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/> , https://www.ncetm.org.uk/media/lp0o2lqv/mastery_assessment_y5.pdf , <https://whiterosemaths.com/resources?year=year-5>

Method:	Concrete:	Pictorial:	Abstract:
To multiply numbers up to 4 digits by a one-digit number using a formal written method	*Concrete resources such as place-value counters, partitioning diagrams and tens-frames can be used to help pupils understand calculation strategies and make connections between known facts and related calculations. However, pupils should not rely on such representations for calculating. Pupils should instead be able to calculate by verbalising the relationship	Children can use own jottings to support their working out so long as knowledge of unitising is used. 	
To multiply numbers up to 4 digits by a two-digit number using a formal written method, including long multiplication for two-digit numbers	As above if needed.	Most children will not need images to support at this point but grid method can be used if needed: 	$\begin{aligned} 124 \times 26 &= 124 \times 20 + 124 \times 6 \\ &= 124 \times 2 \times 10 + 124 \times 6 \\ &= 2,480 + 744 \\ &= 3,224 \end{aligned}$ 

MENTALSTRATEGIES:

- identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers
- pupils should be able to use mixed operation equations to represent the relationships: $5 \times 6 = 3 \times 6 + 2 \times 6$
- Pupils should then use the distributive property and known multiplication table facts to multiply 2-digit numbers (above 12) by one-digit numbers. 14×3 , for example, can be calculated by relating it to 10×3 and 4×3 or partitioned in ways other than into ‘10 and a bit’. For example 14×3 could also be related to double 7×3
- To multiply and divide numbers by 10, 100 and 1000
- Establish whether a number is a prime number (up to 100) or a composite number (not prime) and recall prime numbers up to 19
- To know what a square number is and recall all square numbers (up to and including 144) and know what a cube number is and recall the first 5 cube numbers

Year 6 – Multiplication

Vocabulary: “factor times factor is equal to product”, “The order of the factors does not affect the product.”

Pupils should be able reason in terms of unitising in hundreds, or in terms of scaling a factor by 100:
 “3 times 5 is equal to 15. 3 times 5 hundreds is equal to 15 hundreds. 15 hundreds is equal to 1,500.”
 “If I multiply one factor by 100, I must multiply the product by 100.”

2	Factor
x 5	Factor
10	Product

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-6-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/> , https://www.ncetm.org.uk/media/uitj1x5g/mastery_assessment_y6.pdf , <https://whiterosemaths.com/resources?year=year-6>

Method:	Concrete:	Pictorial:	Abstract:
Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication	*Concrete resources such as place-value counters, partitioning diagrams and tens-frames can be used to help pupils understand calculation strategies and make connections between known facts and related calculations. However, pupils should not rely on such representations for calculating. Pupils should instead be able to calculate by verbalising the relationship	*Children can use own jottings to support their working out so long as knowledge of unitising is used.	$ \begin{array}{r} 124 \\ \times 26 \\ \hline 744 \\ 2,480 \\ \hline 3,224 \\ 11 \end{array} $
multiply one-digit numbers with up to two decimal places by whole numbers	As above	As above	$ \begin{array}{r} 5.35 \\ \times 4 \\ \hline 21.40 \\ 12 \end{array} $ <p>Children can also use knowledge of associated facts and scaling:</p> <p>5.35 x 100 = 535 So 535 x 4 = 2,140 (can be done in a formal method) Then 2,140 ÷ 100 = 21.40</p>



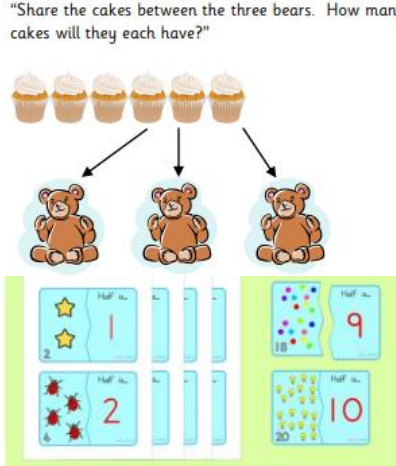

MENTALSTRATEGIES:

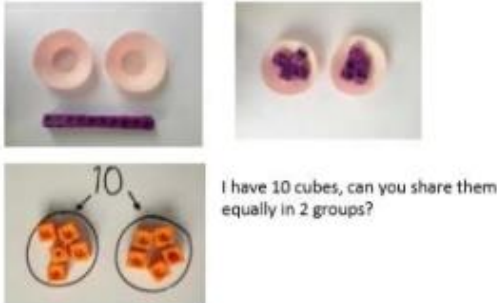
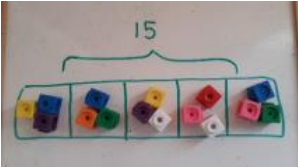
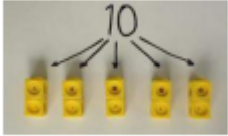

- Secure and maintain fluency in all multiplication tables, and corresponding division facts, through continued practice.
- Identify common factors, common multiples and prime numbers
- Use common factors to simplify fractions mentally
- Use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy



Division Guidance



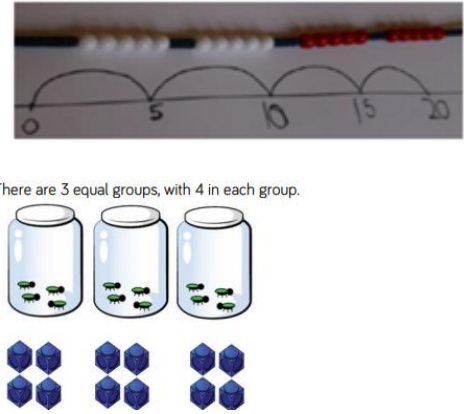
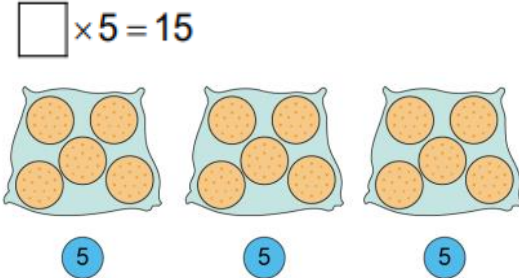
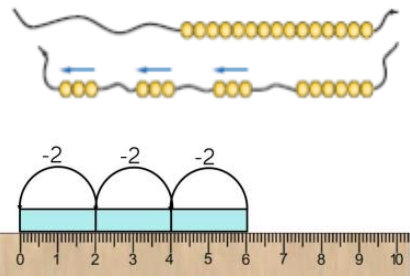
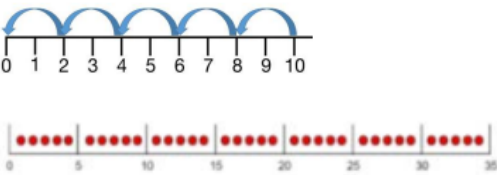
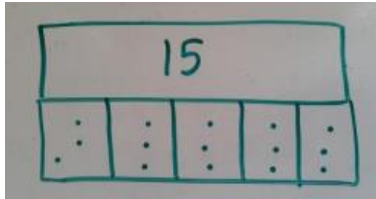
EYFS – Division			
Vocabulary: share, equal, groups,			
Helpful Videos/Resources: https://www.ncetm.org.uk/classroom-resources/ey-numberblocks-support-materials/			
Method:	Concrete:	Pictorial:	Abstract:
<p>Explore and represent patterns within numbers up to 10, including how quantities can be distributed equally.</p>	  <p>Practise sharing range of objects into groups/between children or characters fairly.</p>	<p>Pictorial:</p> <p>"Share the cakes between the three bears. How many cakes will they each have?"</p>  <p>Pictures and icons that encourage children to see concept of halving in relation to subitising, addition and subtraction knowledge. i.e. Knowing 4 is made of 2 groups of 2, so half of 4 is 2.</p>	
MENTALSTRATEGIES:			

Year 1 – Division			
Vocabulary: share, share equally, one each, two each..., group, groups of, lots of, array			
Helpful Videos/Resources: https://www.ncetm.org.uk/classroom-resources/cp-year-1-curriculum-map/ , https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/multiplication-and-division/ , https://www.ncetm.org.uk/media/qjctp24/mastery_assessment_y1.pdf , https://whiterosemaths.com/resources?year=year-1			
Method:	Concrete:	Pictorial:	Abstract:
Through sharing small quantities, pupils begin to understand and division	 <p>I have 10 cubes, can you share them equally in 2 groups?</p>	<p>15 cubes shared between 5 friends. How many does each person get?</p> 	<p>*Pupils do not need to be introduced to the words 'multiplication' and 'division' or to the multiplication and division symbols in year 1 and are not expected to solve calculations presented as written equations.</p>
Through grouping small quantities, pupils begin to understand and division	<p>I have 10 cubes – how many groups of 2 will I have?</p> 	<p>15 cubes into groups of 5. How many groups?</p> 	<p>*Pupils do not need to be introduced to the words 'multiplication' and 'division' or to the multiplication and division symbols in year 1 and are not expected to solve calculations presented as written equations.</p>
MENTALSTRATEGIES: <ul style="list-style-type: none"> - count fluently, both forwards and backwards - sequencing in ones will extend to sequencing in multiples of 2, 5 and 10 - recite the odd number sequence, both forwards and backwards. 			

Year 2 – Division

Vocabulary: share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-2-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/multiplication-and-division/> , https://www.ncetm.org.uk/media/dn0btk14/mastery_assessment_yr2.pdf, <https://whiterosemaths.com/resources?year=year-2>

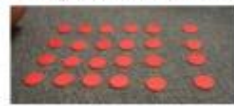
Method:	Concrete:	Pictorial	Abstract:
Recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers	 <p>There are 3 equal groups, with 4 in each group.</p>		<p>Pupils need to be able to solve missing-factor and division problems connected to the 2, 5 and 10 multiplication tables, for example:</p> $\square \times 5 = 20$ $20 \div 5 = \square$ <p>Pupils should solve division (and missing-factor) problems, such as these, by connecting division to their emerging fluency in skip counting and known multiplication facts.</p>
Calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (\times), division (\div) and equals (=) signs		<p>Use a number line to show jumps in groups. The number of jumps equals the number of groups.</p> 	$10 \div 5 = 2$ 

They use commutativity and inverse relations to develop multiplicative reasoning

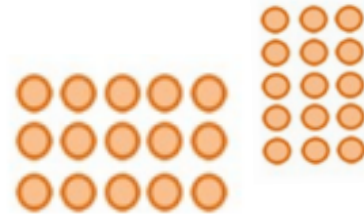
(for example, $4 \times 5 = 20$ and $20 \div 5 = 4$)

Create arrays using counters and cubes and

Numicon.



Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.

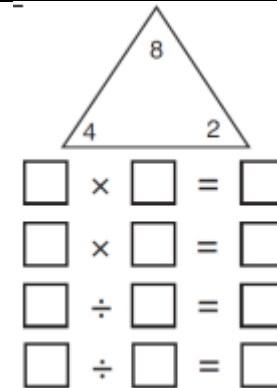


$$3 \times 5 = 15$$

$$5 \times 3 = 15$$

$$15 \div 3 = 5$$

$$15 \div 5 = 3$$



MENTALSTRATEGIES:

- To know that division is the inverse of multiplication
- Recall division facts for the 2, 5 and 10 times tables
- Recall halves for even numbers up to and including 20

Year 3 – Division




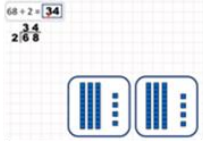
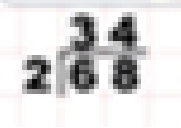

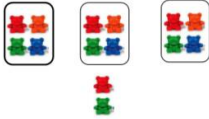



Vocabulary:

Pupils need to use known facts to solve both quotitive (grouping) and partitive (sharing) contextual division problems.
 "7 times 2 is 14, so 14 divided by 2 is 7." "14 divided into groups of 2 is equal to 7." "£14 shared between 2 is equal to £7 each."

$$\text{dividend} \div \text{divisor} = \text{quotient}$$

$$\text{divisor} \overline{) \text{dividend}} \quad \text{quotient}$$

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-3-curriculum-map/>, <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/multiplication-and-division/>, https://www.ncetm.org.uk/media/oagfcvjg/mastery_assessment_y3.pdf, <https://whiterosemaths.com/resources?year=year-3>

Method:	Concrete:	Pictorial:	Abstract:
Children will start to use practical resources to support the short division method	<p>Use cubes, counters, objects or place value counters to aid understanding.</p>  <p>24 divided into groups of 6 = 4</p> $96 \div 3 = 32$ 	 $66 \div 3$  $68 \div 3 = 22 \text{ r } 2$	 $2 \overline{) 34} = 17$
Children will start to use practical resources to support the short division method with remainders	<p>13 ÷ 4</p> <p>Use of lollipop sticks to form wholes- squares are made because we are dividing by 4.</p>  <p>There are 3 whole squares, with 1 left over.</p> $14 \div 3 =$ <p>Divide objects between groups and see how much is left over</p> 	<p>Draw dots and group them to divide an amount and clearly show a remainder.</p>  $69 \div 3 = 23 \text{ r } 2$  $69 \div 3 = 23 \text{ r } 2$	<p>29 ÷ 8 = 3 REMAINDER 5</p> <p>↑ ↑ ↑ ↑</p> <p>dividend divisor quotient remainder</p>  $2 \overline{) 34} = 17$

MENTAL STRATEGIES:

- Count forwards and backwards in multiples of 4, 8, 50 & 100
- Know the division facts from the 3, 4 and 8 times tables
- Use knowledge of place value to calculate division (e.g. $14 \div 2 = 7$, $140 \div 2 = 70$, $1400 \div 2 = 700$)

Year 4 – Division

Vocabulary:

"If we swap the values of the divisor and quotient, the dividend remains the same."

"If the dividend is a multiple of the divisor there is no remainder."

"If the dividend is not a multiple of the divisor, there is a remainder."

"The remainder is always less than the divisor."

dividend ÷ divisor = quotient

quotient
divisor | dividend

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-4-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/multiplication-and-division/> , https://www.ncetm.org.uk/media/x45na0cs/mastery_assessment_y4.pdf , <https://whiterosemaths.com/resources?year=year-4>

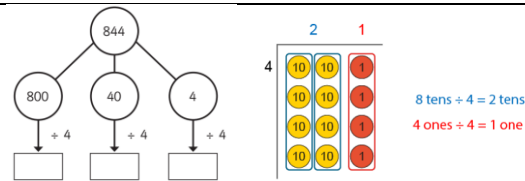
Method:

Solve division problems, with two/three-digit dividends and one-digit divisors

Concrete:

H	T	O
100 100	10	1
100 100	10	1
100 100	10	1
100 100	10	1

Pictorial:



Abstract:

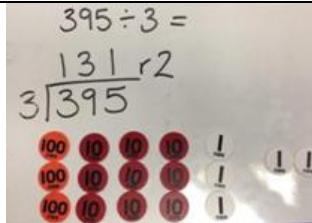
844 ÷ 4 =

$$4 \overline{)844}$$

Solve division problems, with two/three-digit dividends and one-digit divisors, that involve remainders

Tens	Ones
10	1 1
10	1 1
10	1 1
10	1 1

1



$$395 \div 3 =$$

$$131 \text{ r}2$$

$$3 \overline{)395}$$

MENTALSTRATEGIES:

- Recall multiplication and division facts for multiplication tables up to 12×12
- Use place value, known and derived facts to multiply and divide mentally, including: dividing by 1
- Recognise and use factor pairs and commutativity in mental calculations

Year 5 – Division

Vocabulary:

"If we swap the values of the divisor and quotient, the dividend remains the same."

"If the dividend is a multiple of the divisor there is no remainder."

"If the dividend is not a multiple of the divisor, there is a remainder."

"The remainder is always less than the divisor."

"If I make the dividend one-hundredth times the size and the divisor one-hundredth times the size, the quotient remains the same."

$$\text{dividend} \div \text{divisor} = \text{quotient}$$

$$\frac{\text{quotient}}{\text{divisor}} = \frac{\text{dividend}}{1}$$

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-5-curriculum-map/> , <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/> , https://www.ncetm.org.uk/media/lp0o2lqv/mastery_assessment_y5.pdf , <https://whiterosemaths.com/resources?year=year-5>

Method:	Concrete:	Pictorial:	Abstract:																						
Divide numbers up to 4 digits by a one-digit number using the formal written method of short division	<div><div><div><div><div>423 ÷ 3 =</div><div>3 141</div></div><div>Place Value counters: </div></div><div><div><div>423 ÷ 3 =</div><div>3 141</div></div><div>Group the hundreds counters according to the divisor. Write the number of groups above the line in the hundreds column.</div></div><div><div><div>423 ÷ 3 =</div><div>3 141</div></div><div>Exchange the left over 100s counter for ten 10s counters and represent this beneath the line in the tens column.</div></div></div><div><div><div>423 ÷ 3 =</div><div>3 141</div></div><div>Next, group the 10s counters according to the divisor and write the number of groups above the line in the tens column.</div></div><div><div><div>423 ÷ 3 =</div><div>3 141</div></div><div>Group the ones counters according to the divisor and write the number of groups above the line in the ones column.</div></div><div><div><div>423 ÷ 3 =</div><div>3 141</div></div><div>The quotient can be seen across each group</div></div></div>	<div><div>To work out 876 ÷ 4:</div><div>Step 1:<div><div>4 219</div><div>8 7 6</div><div>8 ÷ 4 = 2</div></div></div><div>Step 2:<div><div>4 219</div><div>8 7 36</div><div>7 ÷ 4 = 1 rem 3</div></div></div><div>Step 3:<div><div>4 219</div><div>8 7 36</div><div>36 ÷ 4 = 9</div></div></div><div>So 876 ÷ 4 = 219</div></div> <table><tr><th>x</th><th>4</th></tr><tr><td>1</td><td>4</td></tr><tr><td>2</td><td>8</td></tr><tr><td>3</td><td>12</td></tr><tr><td>4</td><td>16</td></tr><tr><td>5</td><td>20</td></tr><tr><td>6</td><td>24</td></tr><tr><td>7</td><td>28</td></tr><tr><td>8</td><td>32</td></tr><tr><td>9</td><td>36</td></tr><tr><td>10</td><td>40</td></tr></table>	x	4	1	4	2	8	3	12	4	16	5	20	6	24	7	28	8	32	9	36	10	40	<div><div>6 1 9</div><div>8 4,9 15 72</div></div> <div>Within-column calculations:</div> <div>4 ÷ 8 = 0 r 4</div> <div>49 ÷ 8 = 6 r 1</div> <div>15 ÷ 8 = 1 r 7</div> <div>72 ÷ 8 = 9</div>
x	4																								
1	4																								
2	8																								
3	12																								
4	16																								
5	20																								
6	24																								
7	28																								
8	32																								
9	36																								
10	40																								
Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context	<div><div><div>Thousands</div><div>Hundreds</div><div>Tens</div><div>Ones</div></div><div><div><div>3</div><div>2</div><div>4</div></div><div><div>3</div><div>2</div><div>4</div></div><div><div>3</div><div>2</div><div>4</div></div><div><div>3</div><div>2</div><div>4</div></div></div></div>	<div><div>There are 324 chairs to put in the hall. The headteacher wants to put them in 6 rows. How many chairs will be in each row?</div><div>Children could represent it as:</div><div><div>324</div><div>?</div><div>?</div><div>?</div><div>?</div><div>?</div></div></div>	<div><div><div>1</div><div>2</div><div>3</div></div><div><div>4</div><div>8</div><div>9</div><div>14</div><div>12</div></div></div> <div>Pupils do not need to be able to express remainders arising from short division, using proper fractions or decimal fractions</div>																						

MENTALSTRATEGIES:

- identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers
- pupils should be able to use mixed operation equations to represent the relationships: $5 \times 6 = 3 \times 6 + 2 \times 6$
- To multiply and divide numbers by 10, 100 and 1000

Year 6 – Division

Vocabulary:

"If we swap the values of the divisor and quotient, the dividend remains the same."

"If the dividend is a multiple of the divisor there is no remainder."

"If the dividend is not a multiple of the divisor, there is a remainder."

"The remainder is always less than the divisor."

"If I make the dividend one-hundredth times the size and the divisor one-hundredth times the size, the quotient remains the same."

$$\text{dividend} \div \text{divisor} = \text{quotient}$$

$$\frac{\text{quotient}}{\text{divisor}} = \frac{\text{dividend}}{1}$$

Helpful Videos/Resources: <https://www.ncetm.org.uk/classroom-resources/cp-year-6-curriculum-map/>, <https://www.ncetm.org.uk/teaching-for-mastery/mastery-materials/primary-mastery-professional-development/number-addition-and-subtraction/>, https://www.ncetm.org.uk/media/uitj1x5g/mastery_assessment_v6.pdf, <https://whiterosemaths.com/resources?year=year-6>

Method:	Concrete:	Pictorial:	Abstract:																																																																																																
Divide numbers up to 4 digits by a two-digit number using the formal written method of short division and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context	*Concrete resources such as place-value counters, partitioning diagrams and tens-frames can be used to help pupils understand calculation strategies and make connections between known facts and related calculations. However, pupils should not rely on such representations for calculating. Pupils should instead be able to calculate by verbalising the relationship	Pupils will be encouraged to use multiples of the divisor to assist. Eg. <table><tr><th colspan="2">x17</th></tr><tr><td>1</td><td>17</td></tr><tr><td>2</td><td>34</td></tr><tr><td>3</td><td>51</td></tr><tr><td>4</td><td>68</td></tr><tr><td>5</td><td>85</td></tr></table>	x17		1	17	2	34	3	51	4	68	5	85	 																																																																																				
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4	68																																																																																																		
5	85																																																																																																		
Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division	2544÷12 = we can't group 2 thousands into 12s so we will exchange them. 24 hundreds into groups of 12 which leaves 1 hundred. After exchanging the hundred, we have 14 tens. We can group them into 12s and have 2 tens left over. After exchanging the 2 tens, we have 24 ones. We can group them into 2 groups of 12 which leaves no remainders.	<table><tr><td></td><td></td><td>0</td><td>3</td><td>6</td></tr><tr><td>1</td><td>2</td><td>4</td><td>3</td><td>2</td></tr><tr><td></td><td>-</td><td>3</td><td>6</td><td>0</td></tr><tr><td></td><td></td><td></td><td>7</td><td>2</td></tr><tr><td></td><td>-</td><td></td><td>7</td><td>2</td></tr><tr><td></td><td></td><td></td><td></td><td>0</td></tr></table> Multiples of 12: 12 × 1 = 12 12 × 2 = 24 12 × 3 = 36 12 × 4 = 48 12 × 5 = 60 12 × 6 = 72 12 × 7 = 84 12 × 8 = 96 12 × 9 = 108 12 × 10 = 120			0	3	6	1	2	4	3	2		-	3	6	0				7	2		-		7	2					0	<table><tr><td></td><td></td><td></td><td>2</td><td>8</td></tr><tr><td>1</td><td>5</td><td>4</td><td>3</td><td>2</td></tr><tr><td></td><td></td><td>3</td><td>0</td><td>0</td></tr><tr><td></td><td></td><td>1</td><td>3</td><td>2</td></tr><tr><td></td><td></td><td>1</td><td>2</td><td>0</td></tr><tr><td></td><td></td><td></td><td>1</td><td>2</td></tr></table> $\frac{32}{15} = 2\frac{1}{5}$ Answer: $28\frac{4}{5}$ <table><tr><td></td><td></td><td></td><td>0</td><td>3</td><td>6</td></tr><tr><td>1</td><td>2</td><td>4</td><td>3</td><td>2</td><td></td></tr><tr><td></td><td>-</td><td>3</td><td>6</td><td></td><td>↓</td></tr><tr><td></td><td></td><td></td><td>7</td><td>2</td><td></td></tr><tr><td></td><td>-</td><td></td><td>7</td><td>2</td><td></td></tr><tr><td></td><td></td><td></td><td></td><td>0</td><td></td></tr></table>				2	8	1	5	4	3	2			3	0	0			1	3	2			1	2	0				1	2				0	3	6	1	2	4	3	2			-	3	6		↓				7	2			-		7	2						0	
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Use written division methods in cases where the answer has up to two decimal places	As above	*Children can use own jottings to support their working out so long as knowledge of unitising is used.	<table><tr><td></td><td></td><td></td><td>2</td><td>7</td><td>2</td><td>5</td></tr><tr><td>4</td><td>1</td><td>0</td><td>2</td><td>9</td><td>1</td><td>0</td></tr><tr><td></td><td></td><td></td><td></td><td></td><td></td><td>2</td></tr><tr><td></td><td></td><td></td><td></td><td></td><td></td><td>0</td></tr></table> <table><tr><td></td><td></td><td></td><td>2</td><td>8</td><td>8</td></tr><tr><td>1</td><td>5</td><td>4</td><td>3</td><td>2</td><td>0</td></tr><tr><td></td><td></td><td>3</td><td>0</td><td></td><td>↓</td></tr><tr><td></td><td></td><td>1</td><td>3</td><td>2</td><td></td></tr><tr><td></td><td></td><td>1</td><td>2</td><td>0</td><td>↓</td></tr><tr><td></td><td></td><td></td><td>1</td><td>2</td><td>0</td></tr><tr><td></td><td></td><td></td><td></td><td>1</td><td>2</td></tr><tr><td></td><td></td><td></td><td></td><td></td><td>0</td></tr></table>				2	7	2	5	4	1	0	2	9	1	0							2							0				2	8	8	1	5	4	3	2	0			3	0		↓			1	3	2				1	2	0	↓				1	2	0					1	2						0																				
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MENTALSTRATEGIES:

- identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers
- To multiply and divide numbers by 10, 100 and 1000

References

See below the following sources of information that enabled the compilation of this document:

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White Rose Maths:

- <https://whiterosemaths.com/primary-sols/>
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Bar Modelling, Whole School Progression Document – Lois Rooney 2020:

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Michael Drayton Junior School Calculation Policy:

- <https://primarysite-prod-sorted.s3.amazonaws.com/michael-drayton/UploadedDocument/dbff55077953472191f037b31c642383/1.calculation-policy-2020.pdf>

Old Oak Primary Calculation guidance:

- <https://www.oldoakprimary.co.uk/ckfinder/userfiles/files/White-Rose-calculation-policy.pdf>